Consumer Search and Automobile Dealer Co-Location*

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Abstract

Retailers co-locate with rivals to take advantage of economies of agglomeration even though co-location implies greater competition. Using data on all new car transactions registered in Ohio from 2007 to 2014, we estimate a structural model of consumer search for spatially differentiated products that explicitly captures the agglomeration and competition effects of retail co-location. Search frictions generate an average of $333 per car in dealer markups. Agglomeration implies that dealer closures could harm incumbent co-located dealers, even though the incumbent dealers would face less competition. Our results inform the recent policy debate surrounding the massive downsizing of car retail networks and highlight the role of contagion in brick-and-mortar retailing.

*We thank Simon Anderson, Panle J. Barwick, Ying Fan, Paul Grieco, Jean-Francois Houde, Peter Newberry, Regis Renault, John Rust, Henry Schneider, Steven Stern, Matthijs Wildenbeest, Mo Xiao, Daniel Xu, and seminar participants at IIOC, Cornell, Shanghai University of Finance and Economics, and Stony Brook University, for useful discussions and comments. The authors are solely responsible for all errors.

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1 Introduction

Economists and marketers have long sought to understand the location decisions of retail stores and the effects of these decisions on industry profits and consumer welfare. Particular attention has been paid to why retailers tend to locate near each other even though co-location implies fiercer competition. A classic explanation is related to consumers' limited information, for example, as in Stahl (1982) and Wolinsky (1983). If consumers must engage in costly search in order to resolve informational problems before purchase, then they are more likely to search areas where there is a concentration of stores in order to limit their search costs. Consumer search creates an agglomeration benefit for retailers to co-locate. However, co-locating with rival stores could intensify price competition, potentially outweighing the agglomeration benefit from co-location.

In this paper, we empirically study the underlying demand-driven reasons of retail co-location in the new car retail industry. In particular, we examine the extent to which the agglomeration and competition effects are related to consumer search. To do this, we present a structural model of consumer search for spatially differentiated products. In the model, consumers have limited information about their demand for new cars, but can learn their exact valuation of a car by paying a search cost to visit a geographic cluster of new car dealers. This search cost depends on the cluster size and the distance between the consumer's residence and the center of the dealer cluster. After visiting a dealer cluster, consumers learn their exact utility from all cars sold in the geographic cluster. Consumers optimally choose which clusters to search and, conditional on a search, they choose their best option among the searched products. The model gives rise to a positive or negative agglomeration effect of dealer co-location: clusters with more dealers can be more or less likely to be searched by consumers. Whether a positive agglomeration effect exists is an empirical question and whether this agglomeration effect, if positive, dominates the competition effect is an empirical question and depend son model primitives that we estimate.

To estimate the model, we construct a dataset that includes all new car sales registered in Ohio from 2007 to 2014. For each registration, we know the make (brand), model, model year, transaction price, transaction date, identity and location of selling dealer, and the zip code of the buyer's residence. The detailed spatial nature of the data allows us to accurately capture the spatial demand substitution patterns that underlie the demand-driven motives of retail co-location. We estimate a positive agglomeration effect on consumer search. Our estimation results suggest that the car price needs to be $45 lower on average to compensate consumers from traveling an additional mile to search a dealer cluster, although consumers would need to be compensated less for traveling to clusters that contain a greater number of available products. We also find that the consumer search frictions generate $333 on average in markups per car for car dealers and there is significant heterogeneity in these information rents.

Although we estimate a positive agglomeration effect on the demand for vehicles, it is not clear if dealers would prefer to locate near each other because having closer rivals implies fiercer price competition. To understand the balance between agglomeration and competition, we decompose these effects in counterfactual scenarios where dealers are closed. In one counterfactual, we close a

large "anchor" dealer. In another, two car brands, Pontiac and Saturn, are each shut down (before their actual dissolutions). Co-located dealers are harmed through the agglomeration effect because fewer consumers will find that location desirable to search. However, dealer closures help co-located dealers through the typical competition effect: fewer close rivals imply less price competition. To decompose these two effects, we predict what would happen after closures if we forced consumers to choose another car within the same geographic cluster, and then allow the consumers to re-optimize their choice set.

In all counterfactuals, the agglomeration effect hurts co-located rivals after the dealer closure, but it is not always the case that the dealers are worse off because competition is also softened. In the cases of both Pontiac and Saturn closures, our estimates suggest that the agglomeration effect harms neighboring dealers. However, we find that in the case of Pontiac closures, the competition effect dominates the agglomeration effect, and nearby dealers are better off. In the case of Saturn closures, we conclude the opposite, that nearby dealers are worse off after Saturn dealership closures. Our findings have implications for policymakers and managers. In a case when the agglomeration effect dominates the competition effect, it would be in the interest of both local urban planners and the retailers themselves to organize clusters of retail outlets. We show that in the case of car dealers, this is a possible scenario. Also, if the agglomeration effect dominates, this would exacerbate contagion in local economies because one store's closure is more likely to lead to other closures. Additionally, the results suggest that retail managers benefit from the nearby presence of rivals.

The new car retail industry is an ideal setting for such a study. First, it is a large industry with ubiquitous retail co-location. For example, in Ohio (the geographic region of the data we use in our study) more than 85% of new car dealers are located within half a mile of a rival dealer. Along with the results of our structural model, we present evidence from car purchase patterns that illustrate the importance of retail co-location and consumer search in this industry. Second, the automobile industry has experienced massive retail closures over the past half-century. In particular, car dealer closures became a debated policy question during the most recent U.S. financial crisis. During the Troubled Asset Relief Program (TARP), which provided billions of dollars in aid to the U.S. automobile manufacturing industry, Congress, state dealer associations, and car manufacturers battled over the legalities and policy implications of proposals by General Motors and Chrysler to close thousands of franchised new car dealers. However, little is known empirically about the local microeconomic ramifications of retail closures. Our study helps fill the gap of the literature and sheds some light on this policy debate.

Most of prior studies on retail co-location have inferred the agglomeration-competition tradeoff from the revealed entry and location decisions of profit-maximizing retailers. Some of these studies have found that the competition effect dominates, for example, Seim (2006), Jia (2008), and Zhu and Singh (2009); as a result, retailers prefer to differentiate locations and the implication is that a retailer's exit would benefit other incumbents. On the other hand, Vitorino (2012) finds evidence that the agglomeration effect dominates in shopping malls, Ellickson et al. (2013) find that there

exists a net positive agglomeration effect in the big-box retail industry, and Datta and Sudhir (2013) find evidence of the agglomeration benefits of retail co-location using variation in zoning laws. In our paper, we present and estimate a structural model of consumer search for spatially differentiated products, thus specifically modeling the demand-side mechanism for the agglomeration benefits of retail co-location.

Our paper also contributes to the burgeoning literature on empirically understanding limited consumer information. For example, Sovinsky Goeree (2008) estimates a model where advertising affects the choice sets of consumers and show how limited consumer information contributes to firms' market power. Much of this literature has used costly consumer search to explain limited consumer information, including Mehta et al. (2003), Hong and Shum (2006), Wildenbeest (2011), Seiler (2013), Honka (2014), and others. We differ from previous studies by explicitly modeling the spatial co-location of products, and showing how consumer search implies an agglomeration effect of retail co-location. Our model is closely related to the prior literature on consumer search. Both De los Santos et al. (2012) and Honka and Chintagunta (2016) analyze data on consumer actual searches for consumption goods and find that the simultaneous search strategy matches their data better than the sequential search strategy. Without appropriate data to test different search models, we follow Honka (2014) and Moraga-González et al. (2015) by assuming that consumers adopt the simultaneous search strategy to search for new cars.

Our model closely follows Moraga-González et al. (2015) who develop and estimate a structural model of consumer search for new cars in the Netherlands. There are two main differences between our set-up and theirs: (i) in our model, search occurs at the level of a geographic dealer cluster instead of a single dealer; (ii) we estimate the variance of search cost shock which is crucial to quantifying agglomeration and plays a similar role to the nesting parameter in a nested logit framework. On the first point, we validate this assumption by estimating the importance of cluster size in the search cost and presenting descriptive statistics that dealer co-location helps explain purchase behavior. On the second point, we also allow for agglomeration at the cluster level to be zero or negative by including a term that captures cluster size, which we use to test our particular assumption about the nature of search in this market. Also, estimating the variance of search is crucial for understanding agglomeration as the agglomeration effect dominates the competition effect for specific values of the variance parameter.[1] An additional point of contrast between our paper and theirs is that we use individual purchase data, so we observe precisely how far consumers travel to purchase cars. Accordingly, we use the Goolsbee et al. (2004)'s two-step simulated maximum likelihood method to estimate the non-linear parameters of the model.

Lastly, our counterfactual analysis contributes to the literature on retail closure and brand termination. Benmelech et al. (2014) use data across retail industries to estimate the effect of closures due to chain level financial problems on the closure decisions of close-by incumbent retail outlets. They find that nearby retail outlets are more likely to close after a retailer's closure, which

[1] In an updated version of their paper, Moraga-González et al. (2017) estimate a sequential search model using the same automobile data. One result from this exercise is that the their expression for choice probabilities looks very similar to the expression in the case of simultaneous search.

they interpret as evidence of agglomeration effects of closures of bankrupt firms' stores on non-bankrupt incumbent stores. Ozturk et al. (2016) examine the effect of Chrysler dealer closings on the prices of nearby dealers using a national sample of new car transactions in a differences-in-differences framework. They find that after the closures, nearby dealers experience a lower price increase than distant dealers, which is evidence that the agglomeration effect exists in car-buying. Different from the existing studies in this field, we develop a structural model in which either positive or negative agglomeration effects can present and quantify the effects of closures by decomposing the competition and agglomeration effects.

2 Data and New Car Retail Industry

We combine several data sets for our analysis. Our primary data includes detailed records of all new vehicle transactions that ware registered in Ohio from 2007 to 2014. The second data source provides general information on characteristics of all vehicles sold during this time period, and the third data source provides information on all new car dealerships in Ohio. We also use American Community Survey data from the U.S. Census to measure the local demographics at the zip code level.

2.1 Data Description

The primary data is obtained from the Ohio Department of Motor Vehicles (DMV) and consists of all new vehicle transactions initially registered in Ohio from 2007 through 2014. For each transaction, we know the brand (car make), model, model year, transaction price, and transaction date. We also know the identity of the selling dealer, and the five-digit zip code of the buyer.

Throughout the paper, we define a product by car model and model year, for example, Toyota Camry 2010 model. In total, the data includes 1,892 products. We make a number of sample selection decisions for the raw data. First, we remove all commercial vehicles, motorcycles, trailers, and consumer pickup trucks.[2] Second, we drop the products with average prices above $70,000 and small dealers with annual sales below 100 units. These account for around 4% transactions over the eight years. In the end, we are left with more than 2.5 million new car transactions of 34 brands sold by 970 dealers. We define a dealer is defined as a particular brand franchise at a particular location.

We merge the transactions data with information on car characteristics from *edmunds.com*. We use three commonly used characteristics to define the characteristics of a car: acceleration (horse power divided by weight), miles per dollar (miles per gallon divided by dollars per gallon), and the size of the car (length multiplied by width and height). We also dichotomize cars into luxury and

[2] It is common in the literature to consider pickup trucks a different market. Additionally, some models of pickup trucks have dozens of trim levels that vary widely in price and characteristics, making it problematic to aggregate to the model level.

non-luxury brands, and U.S. and non-U.S. brands.[3] Table 1 presents the descriptive statistics of the 2.5 million transactions included in our sample. The average transaction price is $28,253 with a standard deviation is $11,318. Among all new cars registered in Ohio over these eight years, 11% of them are luxury brands and 45% are U.S. brands.

Table 1: Summary Statistics of New Car Transactions in Ohio from 2007 to 2014

Variable	Mean	SD	Min	Median	Max
Transaction price	28,253	11,318	15,312	25,794	65,965
Acceleration	5.91	1.57	2.85	5.57	11.08
Car size	0.84	0.14	0.52	0.81	1.50
Miles per dollar	8.07	1.72	3.63	7.90	17.46
Luxury Brand	0.11	0.31	0	0	1
U.S. Brand	0.45	0.50	0	0	1

Note: Our selected sample includes 2,503,734 new car sales in Ohio from 2007 to 2014, accountng for 101,371 product-dealer-year combinations. Acceleration is the ratio of horse power over the curb weight. Miles per dollar is the average of highway and local miles per gallon divided by gasoline price per gallon in dollars. Car size is the multiplication of car length, width, and height, measured in 100 inches.

Table 2 reports the demographics at the zip code level in Ohio from 2007 to 2014 that we will use in our following analysis, including the median household income in thousands of dollars, share of college degree or higher, number of households, average household size, share of households with children, and the share of urban area. Overall, there is substantial variation for all variables across zip codes. There is also substantial upwards trend in income over our sample.

Table 2: Local Demographics in Ohio by Zipcode by Year

	Mean	SD	Min	Median	Max
Median household income ($000s)	48.28	14.05	10.06	47.23	140.56
Share of college degree or above	0.19	0.12	0.03	0.15	1
Number of households	3,850	4,932	0	1,515	26,802
Average household size	2.54	0.34	1.01	2.52	12
Share of households with children	0.30	0.07	0.01	0.29	1
Share of urban area	0.43	0.43	0	0.34	1

Note: The statistics are calculated based on the demographics of all Ohio zipcodes from 2007 to 2014, including 9,418 unique zipcode-year combinations. Data source: American Community Survey.

2.2 New Car Retail Industry

Table 3 presents the statistics of the top ten brands, including the market share in terms of the total units sold, number of active dealers in Ohio from 2007 to 2014, share of single-brand dealerships, and the average transaction price. The top four brands, Honda, Chevrolet, Ford, and Toyota, accounted

[3]Luxury brands include Acura, Audi, BMW, Buick, Cadillac, Infiniti, Lexus, Lincoln, Mercedes-Benz, Porsche, and Volvo. US brands include traditionally US brands that are no longer U.S. owned, like Chrysler.

for half of the new car sales in Ohio during this time period. 611 of the 970 dealers (63%) sell only one brand. The share of single-brand dealers varies significantly across brands. For example, among all 55 dealers that sell Honda models, 46 of them (84%) sell Honda cars exclusively. In contrast, only 4 out of 119 dealers selling Jeep are single-branded. Along with geographic co-location, multiple-brand dealers is an important aspect of agglomeration in this industry.

Table 3: Top Ten Brands

	Share of units sold	No. of dealers	Single-brand dealers		Ave. trans. price
Honda	14%	55	46	84%	$25,687
Chevrolet	13%	204	145	71%	$26,222
Ford	13%	162	126	78%	$27,097
Toyota	10%	53	17	32%	$25,754
Kia	5%	45	29	64%	$22,759
Hyundai	5%	42	25	60%	$22,984
Nissan	5%	44	31	70%	$26,202
Jeep	4%	119	4	3%	$30,334
Dodge	3%	114	13	11%	$26,838
Subaru	3%	27	13	48%	$25,777
All	100%	970	611	63%	$27,957

Note: The statistics are calculated based on all new car sales that were registered in Ohio from 2007 to 2014. The sample selection is described in the text. Data source: Ohio Department of Motor Vehicles. The number of dealers any given year is less than the total active dealers reported in Table 3 due to industry churn – primarily exit of Pontiac, Saturn, and other U.S. dealers and entry of foreign dealers.

Table 4 presents the number of active new car dealers, the total units sold, and the average transaction price in Ohio from 2007 to 2014. The new car sales dropped dramatically during the financial crisis and this drop was particularly sever for U.S. brands. Along with the sales drop, the number of active dealerships dropped from 759 in 2007 to 635 in 2010 (16% drop). In particular, the number of dealers selling U.S. brand dropped from 510 in 2007 to 379 in 2010 (26% drop), and the total units sold of U.S. brands dropped by 30% during this time period.

Recent car dealer closures stemmed from two primary causes. First, American manufacturers discontinued a number of brands in the mid to late 2000s, starting with Oldsmobile in 2004, and continuing with Saturn and Pontiac in 2009, Mercury in 2010, and Saab in 2011.[4] These brands had seen steady declines in sales, and were reported as being unpopular and out of touch with consumer needs in media and industry reports.[5] In Ohio, due to the terminations of product lines, 83 dealers stopped selling Pontiac, 20 dealers stopped selling Saturn, 42 dealers stopped selling Mercury, and 8 dealers stopped selling Hummer. For the case of GM owned Pontiac and Saab, there was also pressure from the U.S. government, who provided a large loan to GM in 2009 under the Troubled Asset Relief Program (TARP), to make the company "leaner" and more focused on

[4]Saab, the major Swedish produced car brand, was owned by General Motors until 2011. After 2011, the company re-organized, and started producing cars again in 2014.

[5]http://tinyurl.com/cotzn9

core products that had a history of satisfactory sales and performance. The second cause of the dealer closures had to do with the financial crisis more directly. GM and Chrysler received TARP U.S. government loans in 2009, and because of that their subsequent reorganization were allowed to terminate dealers.[6] In our counterfactual exercises, we will examine the effects of dealer closures and offer an explanation of why even unclosed dealers might prefer other dealers not to close. We will also show that the gain of rival dealers is exaggerated by the standard full-information demand model.

Table 4: New Car Dealerships, Sales, and Price in Ohio from 2007 to 2014

	Number of dealers			Total units sold (000)			Average transaction price		
Year	All	U.S.	Non-U.S.	All	U.S.	Non-U.S.	All	U.S.	Non-U.S.
2007	759	510	352	295	138	157	$26,143	$26,339	$25,972
2008	738	477	357	299	131	168	$25,942	$26,168	$25,767
2009	666	410	320	233	96	137	$26,539	$27,386	$25,948
2010	635	379	290	267	138	159	$27,710	$28,905	$26,902
2011	677	416	296	321	145	176	$28,388	$29,075	$27,821
2012	689	416	305	345	151	192	$28,566	$29,323	$27,970
2013	693	421	305	368	165	202	$29,293	$30,092	$28,641
2014	690	416	309	376	173	203	$29,798	$30,736	$29,002

Note: The statistics are calculated based on all new car sales that were registered in Ohio from 2007 to 2014. The sample selection is described in the text. Data source: Ohio Department of Motor Vehicles.

2.3 Spatial Distribution of Ohio Car Dealerships

We group the 970 dealerships into 248 clusters by using the Density-Based Spatial Clustering of Applications with Noise algorithm (DBSCAN). The DBSCAN algorithm is ideal for grouping retail locations, as the objective is to partition points into dense regions separated by non-dense regions. Importantly, the algorithm allows some points to be unclassified – so called "noise points." Because there are many isolated car dealers in Ohio, we added a pre-classification stage to the DBSCAN algorithm where we combined dealers at very similar locations (i.e in the same city block or multi-branded dealerships located at the same address) into a single observation and pre-classified all observations that are more than 10km from the next closest dealer as an isolated dealer.[7]

Figure D.2 in the Appendix 6 displays the spatial distribution of dealership clusters using the DBSCAN algorithm. Among these 970 dealers, 74 of them are grouped into single-dealership clusters, and the remaining 916 dealers are grouped into 248 multi-dealer clusters. Because Ohio is

[6] Both companies, along with Ford Motors, had a clear policy to create smaller dealer networks, but were generally unable to do so because state regulations prohibit dealer franchise contract termination by manufacturers in the automobile industry. Dealers lobbied against dealer closures, citing existing state regulations that prohibit closures. Many of the proposed closures (from both of the reasons stated above) went into legal arbitration. For example, when GM closed the Oldsmobile brand, they reportedly paid over $1 billion to their dealers. For a deeper discussion of the political economy, see Lafontaine and Morton (2010). For example of popular press coverage of dealer closures, see http://tinyurl.com/p7zvgys.

[7] In principle, DBSCAN can handle these isolated dealers and classify them as noise, but the algorithm seemed much more robust to parameter choices when we pre-classified isolated dealers in this manner.

a large state, it is difficult to get a sense of the clustering results without zooming into to particular geography. In Figure B.3, we display the clustering results for four different cities/towns in Ohio. Each color represents a different cluster except orange, which in every case represents separate clusters. Each point may contain many dealer/brands, and the number of brands for each point is displayed below the marker.

Table 5 reports the descriptive statistics at the cluster-year level. On average, a cluster includes 3 physical dealers offering 35 car models of 4 brands and selling 1,403 cars annually. There is significant heterogeneity across clusters. The smallest cluster only includes one dealer offering one brand and selling 50 cars a year, whereas the largest cluster includes 19 dealers offering 188 car models of 25 brands and selling 16,909 a year.

Table 5: Descriptive Statistics of Dealership Clusters

	Mean	SD	Min	Median	Max
No. of dealers	3	3	1	2	19
No. of brands	4	4	1	3	25
No. of models	35	34	3	22	188
No. of products	56	55	4	35	307
No. of units sold	1,403	2,263	50	456	16,909

Note: The statistics are calculated based on 248 dealer clusters in Ohio from 2007 to 2014, 1,784 cluster-year combinations in total. Product is defined at the car model-model year level (e.g., Toyota Camry 2010 model).

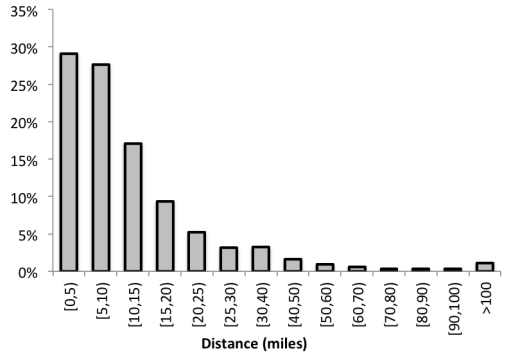
2.4 Consumer Travel and Dealer Co-location

In this section we present new car buyers' choice of dealers and their travel patterns. Figure 1 (a) is a histogram of the distance from a buyer's residence to the dealer they purchased from. The average travel distance is 13.2 miles, the standard deviation is 18.5 miles, and the median is 8.4 miles. 29% of the Ohio new car buyers traveled less than 5 miles to buy their cars, 28% traveled more than 5 but less than 10 miles, 17% traveled more than 10 but less than 15 miles, and the remaining 26% traveled more than 15 miles. In particular, 90% buyers traveled less than 27 miles and 95% buyers traveled less than 40 miles.

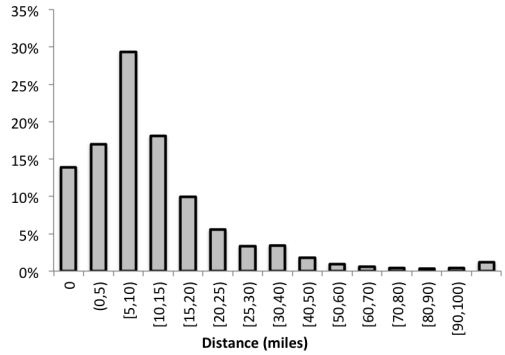
Figure 1 (b) is a histogram of the extra distance that buyers traveled passed the closest dealer cluster. Only 14% of the Ohio new car buyers bought their cars from the nearest dealer clusters, 17% traveled less than 5 miles beyond their nearest clusters, 29% traveled more than 5 miles but less than 10 miles beyond their nearest clusters, and the remaining 40% traveled more than 10 miles beyond their nearest clusters. Our hypothesis is that one reason consumers travel is because the distant cluster that they choose offers more variety or lower price, and they have limited ability to search all clusters, which we explore further next.

Figure 1: Distribution of Travel Distance

(a) Purchase Distance



(b) Distance Passed the Closest Cluster



Note: Travel distance refers to the distance between a new car buyer's residence to the selling dealer's address. Figures are drawn based on 2,503,734 new car transactions in Ohio from 2007 to 2014. Sample selection is described in text. Data source: Ohio Department of Motor Vehicle.

Lastly, we present evidence that dealer co-location is important for consumer demand. To do this, we run a regression where the dependent variable is the distance a consumer traveled to purchase a car and the key explanatory variable is the size of the geographic cluster in terms of the number of dealers where the car was purchased. The hypothesis is that consumers will travel further to purchase cars from larger dealer clusters if dealer co-location is an important factor in the purchase decision. The results are presented in Table 6. In the first column, we control for the buyer zip code. In the second column, we additionally control for the make of the purchased car. The buyer zip-code effects controls for differences in retailing environment faced by different consumers. For example, rural consumers will tend to travel farther just because dealer density is low in rural areas, and these consumers will also face dealers that tend to be less co-located with other dealers. We control for the car make because different makes have different retail network densities. US brands are generally associated with lower travel distances because the retail networks are more dense. In both regressions, we find that longer purchased travel distances are associated with cars located in geographic clusters with more dealers. This is evidence that consumers value dealer co-location. The model we present in the next section provides a formal mechanism for this result.

Table 6: Regression: Travel Distance and Cluster Size

Dep. Variable: Purchase Travel Distance	(1)	(2)
Num. of Co-located Dealers	0.165	0.139
	(0.002)	(0.002)
Constant	11.954	14.417
	(0.0213)	(0.107)
Buyer Zip-code Effect	Yes	Yes
Car Make Effect	No	Yes
R-squared	0.083	0.090
Observations	3,005,651	3,005,651

Note: Unit of observation is an individual car transaction from Ohio between 2008 and 2014. The dependent variable is the distance from the buyer's residence to the dealer. "Num. of Co-located Dealers" is the number of dealers in the same geographic cluster as the selling dealer, where clusters are defined the same way as in Section 2.3.

3 Demand Model

We consider a market where differentiated cars are sold by many geographically dispersed dealers to geographically dispersed consumers. Consumers have limited information about the utility they derive from each car, and must engage in costly search in order to resolve uncertainty before purchase.

3.1 Utility

We use subscript i to denote consumer, subscript z to denote zip code, subscript j to denote product (for example, model year 2016 Honda Accord 2016), subscript f to denote dealer (for example, "Bob's Honda Sales"), and subscript t to denote year. The indirect utility that consumer i living in zip code z derives from product j sold by dealer f in year t is

$$u_{izjft} = \mathbf{x}_{jt}\tilde{\boldsymbol{\beta}}_{izt} - \tilde{\alpha}_{izt}p_{jft} + \varphi_f + \tau_t + \xi_{jft} + \varepsilon_{izjft}, \tag{1}$$

where $\mathbf{x}_{jt}$ is a $K \times 1$ vector of observed car attributes including acceleration (horse power/curb weight), miles per dollar, car size, body style, an indicator of a luxury brand, and an indicator of a U.S. brand, p_{jft} is the average price of product j sold by dealer f in year t, φ_f are dealer-specific effects, τ_t are the yearly dummies, and ξ_{jft} is an unobserved term at the product-dealer-year level. Notice that we include dealer effects and year dummies in the utility so that ξ_{jft} only captures transitory demand shocks. ε_{izjft} is an idiosyncratic match value that can be ascertained only upon visiting the dealer, including the fit and comfortability, personal image of the car, and the specific way that salespeople in the dealership sell the car. Random coefficients $\tilde{\boldsymbol{\beta}}_{izt}$ and $\tilde{\alpha}_{izt}$ that capture consumer heterogeneity in tastes for product attributes and price are assumed to take the following

form:

$$\begin{aligned}\tilde{\beta}_{kizt} &= \bar{\beta}_k + \boldsymbol{H}^x_{zt}\boldsymbol{\beta}^x_k + \sigma^x_k \varsigma^x_{kizt},\ for\ k = 1, ..., K \\ \tilde{\alpha}_{izt} &= \bar{\alpha} + \alpha^{inc} y_{zt} + \sigma^p \varsigma^p_{izt},\end{aligned} \tag{2}$$

where $\boldsymbol{H}^x_{zt}$ is a vector of demographics at consumer's residence zip-code z in year t that affects her preferences, y_{zt} is the log of the median household income in zip-code z in year t, and ς^x_{kizt} and ς^p_{izt} are assumed to follow standard normal distribution identically and independently distributed across characteristics and consumers, denoted as $F_{\boldsymbol{\varsigma}}(\cdot)$.

Let δ_{jft} denote the mean utility across consumers of product j sold by dealer f in year t

$$\delta_{jft} = \mathbf{x}_{jt}\bar{\boldsymbol{\beta}} - \bar{\alpha} p_{jft} + \varphi_f + \tau_t + \xi_{jft}, \tag{3}$$

and μ_{izjft} denote the heterogeneous utility that consumer i living in zip code z obtains from product j sold by dealer f in year t

$$\mu_{izjft} = \sum_{k=1}^{K} x_{kjt}(\boldsymbol{H}^x_{zt}\boldsymbol{\beta}^x_k + \sigma^x_k \varsigma^x_{kizt}) + \left(\alpha^{inc} y_{zt} + \sigma^p \varsigma^p_{izt}\right) p_{jft}. \tag{4}$$

Then, we can write the utility equation (1) as

$$u_{izjft} = \delta_{jft} + \mu_{izjft} + \varepsilon_{izjft}. \tag{5}$$

Consumers have an outside option of not purchasing a new car from a dealer in Ohio. We assume that the utility from the outside choice is $u_{iz0t} = \varepsilon_{iz0t}$, where ε_{iz0t} is assumed to follow a standard type I extreme value (TIEV) distribution, identically and independently across consumers and over years.

3.2 Main Assumptions on Consumer Search

Consumers have the choice to search cars at one or multiple dealer clusters where a dealer cluster represents a geographic area where dealers are co-located. A consumer pays a cost to search a cluster. Before searching, the consumer has expectations about the utility she will derive from each car being sold in a cluster and once the cost is incurred she learns the exact utility from each car in that area. We assume that consumers simultaneously decide the set of clusters to search, and conditional on that search set, they choose the best option. The model is a parametric version of the optimal portfolio choice problem described in Chade and Smith (2006), similar to the consumer search application developed in Anderson et al. (1992) (Chapter 7) that has been recently extended to empirical applications by De los Santos et al. (2012) and Moraga-González et al. (2015).

Simultaneous Search The existing theoretical literature typically models consumer search strategies in two ways. One strand of the literature assumes simultaneous (or non-sequential)

search, where consumers sample a fixed number of sellers and choose to purchase from the most preferred seller among those they have searched.[8] The other strand of the literature assumes sequential search strategy, where after each search consumers choose to purchase from the lowest price observed so far or to make an additional search. Both search strategies have been adopted by empirical researchers. There are two studies we are aware of that test which search model is more consistent with the data in a retail goods setting. De los Santos et al. (2012) analyze a detailed data on the browsing and purchasing behavior of a large panel of consumers and find that the simultaneous search strategy outperforms the sequential search model in their setting. Honka and Chintagunta (2016) also find that the simultaneous search better matches their data on the demand for auto insurance by examining the price variation in consumers' observed considerations sets. Since we do not observe individual consumer's consideration set or search process in our data, we are unable to let the data tell us which search strategy better represents our empirical setting. New car dealers are heavy advertisers, and their locations are usually well marked and near highways or transit thoroughfares. We think it is reasonable that car shoppers are well informed about dealer locations, car features, and other aspects of car buying before they plan shopping trips. Moreover, consumers could easily recall a previously searched car, which would violate an assumption of many sequential search models (see De los Santos et al. (2012)).[9]

Information Set We now explain consumers' information during the search process. First, consumers know the observed and unobserved product attributes at the product-dealer-year level, $(\mathbf{x}_{jt}, \varphi_f, \tau_t, \xi_{jft})$ for all $j,\ f,\ t$ in equation (1). Second, consumers know the average price of each product charged by each dealer in each year, p_{jft} for all $j,\ f,\ t$. This type of information is available on a plethora of car buying websites. Also, advertisements may communicate this information, along with information about dealer specific prices such as a dealer's willingness to give price discounts.[10] Lastly, consumers only know the distribution of the match values ε_{izjft} before search and need to engage in costly search to know the exact values. As is common in the literature, we assume that ε_{izjft} follows a standard TIEV distribution, independently across consumers, products, dealers, and over years.

In our model, the term ϵ_{izjft} captures the information that can be ascertained only upon visiting the dealer. In reality, consumers search may be over these individual match values or over the product prices or some other common attributes. Unfortunately, our data does not allow us to identify the source of consumers' uncertainty. If consumers search to resolve their uncertainty on price, we can interpret the term ϵ_{izjft} as the deviation of a consumer's individual price from the

[8] See Stigler (1961), Burdett and Judd (1983), and Janssen and Moraga-González (2004).

[9] Recently, Moraga-González et al. (2017)show that a version of sequential search can be operationalized in an empirical model of differentiated products demand in a similar way to previous papers that used simultaneous search, including their own earlier manuscript, Moraga-González et al. (2015).

[10] We use the product-dealer-year level average price mainly for two reasons. First, new car retail prices are always set through negotiation and hence may vary across dealers and across consumers. Modeling a bargaining protocol between consumers and dealers would severely complicate our search model. The other reason is a missing data issue. Because car prices are typically negotiated, we only observe the price of the car that a consumer eventually bought but not the the prices of cars that she considered but did not purchase.

average price. Let consumer i (living in zipcode z)'s utility from product j sold by dealer f in year t to be $u_{izjft} = x_{jt}\beta_{izt} - \alpha\tilde{p}_{izjft} + \xi_{jft}$, where $\tilde{p}_{izjft}$ is the individual price that is unknown to consumer i before searching. We can decompose this individual price into two components: $\tilde{p}_{izjft} = p_{jft} + \vartheta_{izjft}$, where p_{jft} is the average price of product j sold by dealer f in year t, and ϑ_{izjft} is i's deviation from the average. If we set $\epsilon_{izjft} = \alpha\vartheta_{izjft}$, the model of searching over match values in the paper is equivalent to this one of searching over price.[11]

3.3 Search and Purchase Decisions

Let $\mathcal{J}_{ft}$ be the set of products from dealer f in year t and $\mathcal{F}_{mt}$ be the set of dealers in cluster m in year t. Let $\mathcal{S}_i$ define consumer i's set of all possible subsets of dealer clusters, with element S. For example, in the two-cluster case, the set of all possible subsets of dealer clusters, $\mathcal{S}$, includes $\{\emptyset\}$, $\{1\}$, $\{2\}$, $\{1\&2\}$, where $\{\emptyset\}$ represents "do not search", $\{1\}$ represents "search cluster 1 only", $\{2\}$ represents "search cluster 2 only", and $\{1\&2\}$ represents "search both clusters". Here, we restrict that consumers never travel further than 40 miles to search for cars, which accounts for 95% of buyers in our sample. As a results, the potential dealer clusters that are considered vary across consumers, depending on which zip code they live in.[12]

The expected gain that consumer i living in zip-code z obtains from a search set $S \in \mathcal{S}_i$ is:

$$\begin{aligned} U_{izt}(S) &= E_\varepsilon\left[max\{u_{iz0t}, \max_{j\in\mathcal{J}_{ft}, f\in\mathcal{F}_{mt}, m\in S} u_{izjft}\}\right] \\ &= ln\left[1 + \sum_{j\in\mathcal{J}_{ft}, f\in\mathcal{F}_{mt}, m\in S} exp(\delta_{jft} + \mu_{izjft})\right], \end{aligned}$$

where the analytic expression exists because the match values ε follows a TIEV distribution.

We define the expected value that consumer i living in zipcode z gets from a search set $S \in \mathcal{S}_i$, denoted as $V_{izt}(S)$, as the difference between her expected gain from S and the searching cost that she needs to pay in order to visit all clusters included in the search set S. Furthermore, we specify the search cost of a search plan S as

$$C_{izt}(S) = \sum_{m\in S} c_{izmt} + \upsilon_{izt} + \omega_{izSt}, \tag{6}$$

where c_{izmt} is the search cost that consumer i living in zip code z needs to pay if she visits a dealer

[11] There are three things worth mentioning about the equivalence of match value and price search. First, to make the two models equivalent, the price coefficients have to be the same across consumers. Second, to make the two models equivalent, either we can assume ϵ_{izjft} follows a standard TIEV distribution and ϑ_{izjft} follows a TIEV distribution with location parameter 0 and scale parameter $1/\alpha$, or we can assume ϑ_{izjft} follows a standard TIEV distribution and ϵ_{izjft} follows a TIEV distribution with location parameter 0 and scale parameter α. Third, searching over prices and searching over match values are not the same if we consider the supply side choices. In theory, variation of transaction price could help identify the source of uncertainty. However, using that variation for identification requires us to incorporate the price bargaining process between consumers and dealers into the model, which is unachievable given our already complicated search model and our lack of search and bargaining data.

[12] This restriction dramatically reduces the computational burden of computing consumers' optimal search set. Otherwise, it is computationally infeasible to compute them by allowing consumers to optimally choose their search sets among 248 clusters.

cluster m in year t, υ_{izt} is an individual-year specific term that captures the search cost shocks associated with that consumer, and ω_{izSt} is an individual-search set-year-specific error term that captures the unobserved search cost shocks such as the traffic condition of that search. We assume that υ_{izt} follows a normal distribution with mean zero and standard variance σ_{υ}^2. If consumer i living in zipcode z does not search any cluster, her expected gain and search cost are normalized to be zeros.

Furthermore, we assume that the search cost of consumer i (living in zip-code z) from visiting a dealer cluster m in year t is

$$\begin{aligned} c_{izmt} &= \gamma_{iz} d_{zm} + \rho n_{mt}, \\ with\ \gamma_{iz} &= \lambda_0 + \boldsymbol{H}_{zt}^c \boldsymbol{\lambda}^H, \end{aligned} \tag{7}$$

where d_{zm} is the distance from consumer i's zip-code to the geographic center of a dealer cluster m, n_{mt} is the number of dealers in that cluster, and $\boldsymbol{H}_{zt}^c$ is a vector of consumer i's zip-code level demographics that may affect her search cost, including the log of median household income, share of urban area, and share of households with children under 18 years old in i's zip-code in year t. Importantly, we include ρ in the model to test whether search happens at the cluster level as we have specified, or search happens at the dealer level, for example as in Moraga-González et al. (2017). The benefits of search already incorporates the number of dealers through $U_{izt}(S)$, so ρ allows for consumers to face additional dealer-specific search costs. captures the fact that search *costs* may be increasing in the number of dealers, which would suggest that consumers also incur some dealer-specific search cost.

Consumer i (living in zip-code z) chooses the search set S^* in year t that gives her the highest expected utility among all possible search sets $\mathcal{S}_i$. That is,

$$V_{izt}(S^*) \quad \geq \quad V_{izt}(S)\, for\, \forall S \in \mathcal{S}_i$$

In our model, the variation in the optimal search sets across consumers is generated by their different valuations for products contained within each search set ($U_{izt}(S)$), their different distances to dealer clusters (d_{zm}), their different demographics ($\boldsymbol{H}_{zt}^c$), the number of dealers in each cluster (n_{mt}), their idiosyncratic cost shocks υ_{izt}, and their different draws of search set specific idiosyncratic cost shocks (ω_{izSt}). The size of a consumer's search cost ultimately determines how many clusters she will search.[13]

However, as pointed out by Chade and Smith (2006), the optimal search set will not necessarily follow a cut off rule of an ordering of $U_{izt}(S)$'s from highest to lowest. Following De los Santos et al. (2012), among others, we analytically compute the probability of choosing each search set by assuming that ω_{izSt} follows a TIEV distribution with a location parameter of zero and a scale

[13] It is also reasonable to think that distance would enter the indirect utility function because it affects the ease of getting the car serviced. However, we do not model this because the distance parameters would only be separately identified from functional form.

parameter of κ.[14] Specifically, the probability that consumer i living in zip code z chooses a search set S is

$$\mathcal{P}_{izSt} = \frac{exp[(U_{izt}(S) - \sum_{m\in S} c_{izmt} - \upsilon_{izt})/\kappa]}{1 + \sum_{S'\in \mathcal{S}_i} exp[(U_{izt}(S') - \sum_{m\in S'} c_{izmt} - \upsilon_{izt})/\kappa]}.$$

Let m^f to denote the cluster of dealer f. The probability that consumer i living in zip code z purchases product j from dealer f in year t conditional on a search set S follows the familiar analytical expression:

$$\mathcal{P}_{izjft|S} = \begin{cases} \frac{exp(\delta_{jft}+\mu_{izjft})}{1+\sum_{j'\in\mathcal{J}_{ft}, f'\in\mathcal{F}_{mt}, m\in S} exp(\delta_{j'f't}+\mu_{izj'f't})}, & if\, m^f \in S \\ 0 & if\, m^f \notin S. \end{cases}$$

Then, the unconditional probability that consumer i purchases product j from dealer f in year t is

$$\mathcal{P}_{izjf}(\boldsymbol{\delta}_t, \mathbf{x}_t, \mathbf{p}_t, \boldsymbol{H}_{zt}, \mathbf{d}_z; \boldsymbol{\theta}_1, \boldsymbol{\theta}_2) = \int \sum_{S\in\mathcal{S}_i} \mathcal{P}_{izjft|S}\mathcal{P}_{izSt} dF_{\boldsymbol{\varsigma}}(\cdot), \tag{8}$$

where $\boldsymbol{H}_{zt} = (y_{zt}, \boldsymbol{H}^x_{zt}, \boldsymbol{H}^c_{zt})$ includes the zip-code level demographics that affect consumer preference and search cost, $\boldsymbol{\theta}_1 = (\boldsymbol{\beta}^x, \boldsymbol{\sigma}^x, \alpha^{inc}, \sigma^p, \boldsymbol{\lambda}, \rho, \kappa, \sigma_\upsilon)$ represents all "non-linear" parameters in the model, and $\boldsymbol{\theta}_2 = (\bar{\boldsymbol{\beta}}, \bar{\alpha}, \varphi_f, \tau_t)$ represents all "linear" parameters in the model.

3.4 Discussion of the Model

3.4.1 Search Cost and Substitution Patterns

Non-trivial consumer search creates particular substitution patterns within and across clusters. All cars within a cluster are either in, or out, of a given consumer's choice set. In this sense, within-cluster substitution between cars is similar to standard full-information BLP models with zero search cost. In our model, however, consumers dislike traveling distance and hence all else equal, they are more likely to visit nearby clusters. Therefore, if two clusters are further away, the products across these two clusters are less substitutable, all else equal.

Particularly, the magnitude of the across-cluster substitution depends on consumer search cost. In our model, the parameter γ measures to what extent consumers dislike traveling distance. Hence, a larger γ implies a lower across-cluster substitution. Similarly, a larger ρ (the coefficient before the number of dealers in a cluster) also implies a larger search cost and hence a lower cross-cluster substitution. Another crucial parameter in our search cost equation is κ, the standard deviation of the idiosyncratic shock to each search set. A larger κ implies more randomness, and hence a lower importance of car attributes and traveling distance in consumers' optimal choice of search set. In other words, a larger κ implies that dealers' location is less relevant and hence the substitution among products in different clusters are more substitutable. In the extreme case when κ is infinite, consumers choose each search set among all possible sets with equal probabilities, and dealers' loca-

[14] The specification is also similar to the limited information model in Sovinsky Goeree (2008), however, in that model choice sets are exogenous to the consumer.

tion will not affect the substitution at all. In this sense, the parameter κ has a similar interpretation as the nesting parameter in a nested logit model if "nests" are defined as geographic clusters. Just like the nesting parameter, κ governs the amount of substitution across dealer clusters, or "nests." As we discuss later, identification of this parameter is akin to identification of the nesting parameter in Berry (1994), or any random coefficient that controls substitution patterns.[15]

3.4.2 Agglomeration, Competition, and the Economics of Retail Closures

In our model, cars in large clusters are more likely to be searched but less likely to be chosen given they are searched. The former happens because consumers find large clusters more attractive (as long as ρ is not too high) and the later happens because large clusters imply more choices and greater competition. Here we explain the agglomeration effect in more detail. Intuitively, the sign and magnitude of the agglomeration effect of dealer co-location are determined by two forces. First, the likelihood that a cluster is visited by a consumer depends on the additional gain by including it into her search set. A cluster with more dealers (and hence more products) is, all else equal, more attractive to consumers and hence more likely to be included in search. This is because a cluster with more products provides a higher chance for a consumer to find a product that has the characteristics she values and also provides more draws of the idiosyncratic shock ϵ_{izjft} and hence a higher maximum order statistics[16]. This is the agglomeration benefit from co-location. However, the likelihood of a cluster is visited by a consumer also depends on the extra search cost if she includes it in her search cost. Most likely, the colocation of more dealers leads to a higher search cost (a positive ρ). In this case, a cluster with more dealers is more costly to be included in the search set and hence less likely to be visited, all else equal. This is the agglomeration cost from co-location. Whether colocation leads to a positive or negative agglomeration effect crucially depends on the value of ρ. If ρ is sufficiently small, the agglomeration benefit tends to outperform the agglomeration cost and hence a cluster with more dealers tends to be more likely visited by consumers. In contrast, if ρ is sufficiently large, a cluster with fewer dealers tends to be more likely included in a consumer's search set.

Our model also clearly predicts how the closure of a dealer affects other co-located dealers in the same cluster. To illustrate this, below we walk through a simpler two-cluster example. Consider two dealer clusters, 1 and 2. n_1 dealers are located in cluster 1 and n_2 dealers are located in cluster

[15] A particularly interesting case is when $\gamma = 0$, $\rho = 0$, and $\kappa = 1$. Let $\mathcal{S}_f$ denote the set of search sets that includes the dealer f's cluster. The individual choice probability in this particular case is

$$\begin{aligned}\mathcal{P}_{izjft} &= \sum_{S\in\mathcal{S}_i} \mathcal{P}_{izjft|S}\mathcal{P}_{izSt} = \sum_{S\in\mathcal{S}_f} \frac{exp(\delta_{jft}+\mu_{izjft})}{\sum_{S'\in\mathcal{S}_i} exp[(U_{izt}(S')]} \\ &= \frac{2^{M-1}exp(\delta_{jft}+\mu_{izjft})}{2^M + 2^{M-1}\left[\sum_{j',f'} exp(\delta_{j'f't}+\mu_{izj'f't})\right]} = \frac{exp(\delta_{jft}+\mu_{izjft})}{e^{ln(2)} + \sum_{j',f'} exp(\delta_{j'f't}+\mu_{izj'f't})}.\end{aligned}$$

Therefore, this case is equivalent to the standard full-information model with mean utility from outside option being $ln(2)$.

[16] This is a well known property of variants of the logit discrete choice model and has the flavor of "love of variety" in representative consumer models. See Anderson et al. (1992) for details of welfare in discrete choice demand models.

2. So the set of possible search sets is $\mathcal{S} = \{\emptyset, 1, 2, 1\&2\}$. For notation simplicity, let u_{if} denote the consumer i's utility from firm f which follows a type I extreme value distribution with location parameter μ and scale parameter 1. For simplicity, assume that consumers have the same search cost to a cluster which is a linear function of the distance and the number of dealers in that cluster, that is, $c_m = \gamma d_m + \rho n_m$. In addition, there exists a search cost shock for each search set, denoted as ω_S, which is assumed to follow a TIEV distribution with location parameter 0 and scale parameter κ.

The expected utility of choosing a search set $S \in \mathcal{S}$ is $U_S = ln(1 + (\sum_{m \in S} n_m)e^{\mu})$ and the search cost is $c_S = \gamma(\sum_{m \in S} d_m) + \rho(\sum_{m \in S} n_m) + \omega_S \equiv \bar{c}_S + \omega_S$. Because of the assumption on the distribution of ω_S, the probability of choosing a search set $S \in \mathcal{S}$ is

$$\mathcal{P}_S = \frac{exp\left[(U_S - \bar{c}_S)/\kappa\right]}{1 + exp\left[(U_1 - \bar{c}_1)/\kappa\right] + exp\left[(U_2 - \bar{c}_2)/\kappa\right] + exp\left[(U_{1\&2} - \bar{c}_{1\&2})/\kappa\right]},$$

and the probability of choosing a dealer in cluster m given a search set S is

$$\mathcal{P}_{m|S} = \frac{e^{\mu}}{exp(U_S)}. \tag{9}$$

Then, the unconditional probability of buying from a dealer in cluster m is

$$\mathcal{P}_m = \sum_{S \in \mathcal{S}_m} \mathcal{P}_S \mathcal{P}_{m|S},$$

where $\mathcal{S}_m$ is the set of search sets that includes cluster m.

We show that our model can predict either positive or negative agglomeration effects, depending on the parameters. Moreover, the sign of the agglomeration effect depends on the number of dealers, which is a way to test whether cluster search costs or dealer-specific search costs are the dominant feature driving search. We define that the agglomeration effect of colocating in cluster m is positive (negative) if $\partial(\mathcal{P}_m + \mathcal{P}_{1\&2})/\partial n_m$ is positive (negative). That is, cluster m is more (less) likely to be visited if more dealers colocate in that cluster.

[Proposition 1]: There exists a positive cutoff ρ_m^* such that the agglomeration effect in cluster m is positive iff $\rho < \rho_m^*$; and negative iff $\rho \geq \rho_m^*$. Moreover, the cutoff ρ_m^* is decreasing in n_1, n_2 and γ, but increasing in μ.

[Proposition 2]: In the case of $\rho < \rho_m^*$ so that the agglomeration effect is positive, there exists a cutoff κ^* such that as κ increases, the agglomeration effect becomes stronger when $\kappa \leq \kappa^*$ and weaker when $\kappa > \kappa^*$.

The proofs of these propositions are in Appendix A. Next we can show the impacts of closing a dealer on other co-located dealers in the same cluster. Closing a dealer in cluster 1 would lower the expected utility of searching cluster 1 through U_1 and the expected utility of searching both clusters through $U_{1\&2}$. Consider an incumbent co-located dealer j in cluster 1. Lower U_1 and $U_{1\&2}$

increase the conditional probability $\mathcal{P}_{j|1}$ and $\mathcal{P}_{j|1\&2}$. That is, closing a dealer in cluster 1 increases the probability of purchasing from a co-located dealer conditional on cluster 1 being searched. This is the competition effect of dealer closure on a colocated dealer. Meanwhile, when ρ is below (above) ρ_1^*, lower U_1 and $U_{1\&2}$ decrease (increase) the probability that cluster 1 is included in consumers' search set, $\mathcal{P}_1 + \mathcal{P}_{1\&2}$. This is the agglomeration effect of dealer closure on a colocated dealer. In the case of $\rho \geq \rho_1^*$, the agglomeration effect is negative and hence the total effect of closing a dealer in cluster 1 would benefit other co-located dealers in cluster 1. However, when $\rho < \rho_1^*$, the agglomeration effect is positive and hence the total effect of dealer closure depends on the size of the agglomeration and competition effects. As κ decreases, for example when it is near or lower than κ^*, the agglomeration effect tends to dominate the competition effect, implying that the closure of a dealer in cluster 1 would worsen off the co-located dealers in cluster 1. This is intuitive, as low κ implies that search is less random and consumers are more willing to substitute across clusters based on cluster characteristics.

4 Estimation and Results

Our estimation procedure follows Goolsbee and Petrin (2004)'s two-step approach. In the first step, we use the individual transaction data to maximize the likelihood function that includes product-dealer-year specific dummies to capture those mean utilities. This identifies all "non-linear" parameters $\boldsymbol{\theta}_1$ and the mean utilities $\boldsymbol{\delta}$. To estimate linear parameters of the model $\boldsymbol{\theta}_2$, in the second step we run a regression of the estimated mean utilities on model-dealer-year characteristics, using instruments to account for correlation of price with the unobserved quality ξ_{jft}.

In the first step, for any candidate value of $\boldsymbol{\theta}_1$ and any vector of product fixed effects $\boldsymbol{\delta}$, the log-likelihood function is

$$logL(\boldsymbol{\delta}, \boldsymbol{\theta}_1) = \sum_{i,z,j,f,t} I_{izjft} \times log \left[\frac{\mathcal{P}_{izjf}(\boldsymbol{\delta}_t, \mathbf{x}_t, \mathbf{p}_t, \boldsymbol{H}_{zt}, \mathbf{d}_z; \boldsymbol{\theta}_1)}{\sum_{j,f} \mathcal{P}_{izjf}(\boldsymbol{\delta}_t, \mathbf{x}_t, \mathbf{p}_t, \boldsymbol{H}_{zt}, \mathbf{d}_z; \boldsymbol{\theta}_1)} \right] \tag{10}$$

where $\frac{\mathcal{P}_{izjf}(\boldsymbol{\delta}_t, \mathbf{x}_t, \mathbf{p}_t, \boldsymbol{H}_i, \mathbf{d}_i; \boldsymbol{\theta}_1)}{\sum_{j,f} \mathcal{P}_{izjf}(\boldsymbol{\delta}_t, \mathbf{x}_t, \mathbf{p}_t, \boldsymbol{H}_i, \mathbf{d}_i; \boldsymbol{\theta}_1)}$ is the probability that consumer i living in zip code z purchases product j from dealer f given that she purchases, and I_{izjft} is an indicator indicating whether consumer i living in zip code z purchases j from f in year t.

Following Goolsbee and Petrin (2004), we do not maximize the likelihood over the entire space of $(\boldsymbol{\theta}_1, \boldsymbol{\delta})$ directly. Instead, we concentrate out the likelihood function and only search over the space of $\boldsymbol{\theta}_1$. To do this, we condition on $\boldsymbol{\theta}_1$ and solve for the vector $\boldsymbol{\delta}_t(\boldsymbol{\theta}_1)$ that matches the observed market shares to those predicted by the model:

$$s_{jft} = \mathfrak{s}_{jf}(\boldsymbol{\delta}_t, \mathbf{x}_t, \mathbf{p}_t; \boldsymbol{\theta}_1) = \sum\nolimits_z \frac{b_{zt}}{B_t} \int \mathcal{P}_{izjf}(\boldsymbol{\delta}_t, \mathbf{x}_t, \mathbf{p}_t, \boldsymbol{H}_{zt}, \mathbf{d}_{zt}; \boldsymbol{\theta}_1) dF(\boldsymbol{\varsigma}_i, \omega_i), \tag{11}$$

where b_{zt} is the number of potential consumers in zip-code z, $B_t = \sum_z b_{zt}$ is the total number of potential consumers, and $F(\cdot)$ is the distribution of random preference to product attributes and

price ς_i and the random search cost term ω_i. This procedure is just the MLE analogy to the GMM procedure proposed in BLP.

After we obtain the estimates of non-linear parameters $\hat{\boldsymbol{\theta}}_1$ from the first step, we compute the mean utilities at the estimated value of $\hat{\boldsymbol{\delta}} = \boldsymbol{\delta}(\hat{\boldsymbol{\theta}}_1)$. In the second step, we estimate $\boldsymbol{\theta}_2$ from equation (3). We construct instruments in a similar spirit to Gandhi and Houde (2016a). For a given car characteristic, we take the squared difference of a particular product with the average characteristic in that product's cluster. We also take this difference with respect to the average characteristic in the entire state of Ohio. Let $\boldsymbol{Z}_{jft}$ denote the vector of all excluded variables including car characteristics $\mathbf{x}_{jt}$, L instrumental variables, dealer fixed effects, and year dummy variables. Our empirical moment conditions for the second stage are

$$G_N(\boldsymbol{\theta}_2) = \frac{1}{N_2} \sum_{j,f,t} \xi_{jft} \mathbf{Z}_{jft}, \tag{12}$$

where N_2 is the number of product-dealer-year level observations.

Notice that the estimation errors of the first stage estimation will be carried into the second stage estimation, implying that we need to correct the standard errors of the second stage estimates.[17] We correct for this additional uncertainty in the second stage estimates and provide the derivation of the asymptotic covariance matrix of the second-stage estimates in Appendix 6.

4.1 Identification

In this section we provide an informal discussion of the model identification. The identification of the parameters in the utility function is similar to the full-information BLP models. They can be identified because we observe different within-cluster market shares corresponding to different product characteristics and different sets of products available across clusters and over time. Also, we also observe consumer-level choices and the variation in their within-cluster choices corresponding to different product characteristics, consumer characteristics, and choice sets also help to identify those parameters in the utility function.[18]

To identify the price coefficients, we need to address the classical endogeneity problem that arises because dealers and consumers observe the unobserved quality when making their decisions and so the average price will adjust to the changes in unobserved quality. Relevant and valid instruments are those variables that are correlated with prices and independent of unobserved transitory demand shocks. Following Nevo (2001), Houde (2012) and Gandhi and Houde (2016b), we use deviations of particular products characteristics from the averages of other products as instruments (see above). Specifically, we include four other groups of instrumental variables: (i) the deviations from the

[17] Thanks to one of our referees for pointing this out.

[18] For the "standard" model, ie BLP, the requirement for identification is that the researcher observes variation in choice sets. In our case, choice sets are endogenous, but we have generous variation in potential choice sets across Ohio, especially when you consider that consumers generally have steep disutility of traveling (something we confirm with our estimates). For example, two consumers in Ohio may face very different retailing environments, depending on where they live, and the this variation exogenously shifts around the choice sets ultimately faced by consumers. We thank a referee for pointing this out.

average characteristics of all other product-dealer combinations available in the same dealer cluster and in the same year, (ii) the squares of the first group variables, (iii) the deviations from the average characteristics of all other product-dealer combinations in the same year, and (iv) the squares of the third group variables. The variation we rely on is variation in the average characteristics across different local geographies in Ohio, which means we rely on the fact that there exists very different dealer networks in different parts of Ohio. This variation should not be correlated with ξ_{jft} particularly because we include dealer effects. We display the results from a regression of price on all of the exogenous variables in Table D.1 in the Appendix 6. Most of the excluded variables are highly significant and the R-squared is 0.72.

The specific search mechanism is not identified per se. Because we do not observe consumer choice sets or search behavior, we cannot reject another search model, for example a full information model or a sequential search model, in favor of our model. Conditional on our parametric assumptions about search, the parameters in the search cost function can be identified from co-variation in individual distance and individual choices in the data. Consider two consumers with similar preferences to product attributes and price. They should have similar expected gain from each search set $U_{izt}(S)$ and similar conditional purchasing probabilities $\mathcal{P}_{izjft|S}$. The distance coefficients, $\boldsymbol{\lambda}$, can be identified from the variation in their choices corresponding to their different distances to dealers and their different demographics affecting their search costs ($\mathbf{H}^c_{zt}$). The cluster size coefficient ρ is identified from co-variation in choices and the size of the chosen dealer's cluster. The identification of κ comes from the variation of individual choices among those consumers with similar demographics and similar distances to dealer clusters. For example, if those consumers make similar choices, then the variance of their search cost shocks κ should be small. In this sense, κplays a similar role to the nesting coefficient in a nested logit model. As choice sets vary across similar consumers, does the researcher observe consumers making similar decisions or apparently random decisions. The variance of ϵ is not identified, as is typical in discrete choice models, and, in turn, κ is not separately identified from the variance of ϵ.

The above argument of the identification of the search cost parameters relies on the assumption that dealer entry, exit, and location choice are not correlated with the unobserved transitory demand shocks, ξ_{jft}, after controlling for dealer and time fixed effects. Because we include dealer and year effects, this assumption is valid if entry decisions are based on the long-run store characteristics and aggregate economic shocks, but not on the realization of the transitory shocks ξ_{jft}. This assumption is reasonable in our context, because the sunk cost involving the entry, exit, and location change of a dealer is substantial, partly due to regulations that limit entry and exit. Forced exit of dealers by the manufacturer is very difficult in this industry because of state laws requiring payments to dealers for termination of franchise contracts. In addition, there are other state laws that make it difficult for entry and exit, including mandated exclusive territories for brands. For a discussion of the regulatory environment see Lafontaine and Morton (2010) and Murry and Schnieder (2016). Also, to the extent the local demographics and population change over time, initial decisions about entry may not reflect current demographics, population, or other transitory factors, see Murry (2018) for

evidence. As discussed in section 2.2, the number of dealers decreased by nearly 9 percent in Ohio during the past financial crisis, creating sharp changes in the structure of local market. Importantly, these changes were driven mainly by the national-wide brand terminations and dealer closure due to car manufacturers' financial crisis, but not by factors related to local transitory demand conditions.

4.2 Model Estimates and Fit

Table 7 reports the estimates of all parameters in our search model. As expected, the estimate of α^{inc} is positive, implying that higher-income consumers are less price sensitive. The implied consumer-model-dealer-year level own-price elasticities of demand range from -10.73 to -1.38, with a sales weighted average of -4.05. This suggests that consumers are price sensitive on average, but there is substantial heterogeneity. Overall, our estimates of price elasticities are consistent with previous studies of automobile demand.[19] As expected, the average consumer prefers cars with higher acceleration (horsepower divided by vehicle weight) and higher miles per dollar. Larger households like larger cars more. Consumers that live in zip-codes with higher rates of education prefer U.S. brand cars less.

The distance coefficients have the expected signs and are precisely estimated. The search cost is increasing in the traveling distance. This relationship is even stronger for households with higher income and children and also stronger for locations with more urban areas and worse traffic conditions. The coefficient before the number of dealers in a cluster (ρ) is almost zero and not significant at 10 percent level. The standard deviation of the search set shock (κ) is estimated to be 0.3716 and is estimated precisely.[20] In the following sections, we will further discuss the implications of the estimated search costs.

[19] For example, the average own-price elasticity is equal to -4.1 in Albuquerque and Bronnenberg (2012), -5.3 in Murry (2015), and -3.14 in Nurski and Verboven (2016).

[20] A previous working paper version of this paper used much less data (four years in a single city in Virginia) to estimate the model, and in that case κ was very weakly identified. This reinforces the idea that variation in choice sets is crucial to identify this parameter.

Table 7: Model Estimates

Variable	Coeff.	Estimate	Std. Err.
Utility Parameters			
Price ($10,000)	$\bar{\alpha}$	-1.4201	(0.0111)
Price×log(income)	α^{inc}	0.1224	(0.0169)
Price – random effect	σ^p	0.1338	(0.0429)
log(Acceleration)	$\bar{\beta}_1$	1.4064	(0.0324)
log(Car Size)	$\bar{\beta}_2$	8.355	(0.0559)
log(Miles per Dollar)	$\bar{\beta}_3$	1.0662	(0.0532)
Luxury Brand	$\bar{\beta}_4$	0.8394	(0.0298)
U.S. Brand	$\bar{\beta}_5$	0.3856	(0.0248)
log(Car Size)×Household Size	β_2^x	1.8612	(0.3883)
log(Miles per Dollar) – random effect	σ_3^x	0.1814	(0.0991)
U.S. Brand×College Degree	β_5^x	-1.0692	(0.4201)
U.S. Brand – random effect	σ_5^x	0.0425	(0.0535)
Constant	$\bar{\beta}_0$	-6.9138	(0.2061)
Search Parameters			
Distance (100 miles)	λ_0	13.6687	(0.6776)
Distance×log(income)	λ_1^H	0.4678	(0.1159)
Distance×Share of Households w. children	λ_2^H	-0.2601	(0.0174)
Distance×Share of Urban Area	λ_3^H	1.7977	(0.4901)
No. of Dealers in Cluster	ρ	0.0014	(0.0020)
Std. Err. of Consumer heterogenity	σ_υ	1.2209	(0.1348)
Std. Err. of search-set heterogeneity	κ	0.3716	(0.0376)

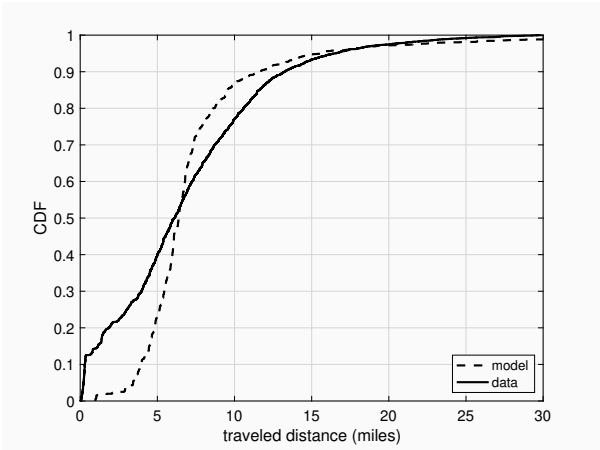
Note: The estimation includes 101,371 model-dealer-year combinations, 9,415 zip code-year combinations, 2,112 dealer cluster-year combinations, and 8,000 individuals. The mean utility function also includes body style dummies, dealer fixed effects, and yearly dummies. Average transaction price is measured in $10,000. Distance between a consumer zip code to a dealer cluster is measured in 100 miles.

To examine the fit of the model, we simulate the choices of those buyers who we have used to construct the likelihood function in the first stage estimation. Figure 2 presents the cumulative distributions (CDF) of the model predicted purchase travel distance and the distance observed in the data. Our model predicts that the average distance is 7.42 miles and the standard deviation is 4.81 miles, whereas the average distance is 6.80 miles in our estimation sample and the standard deviation is 5.20 miles. Overall, our model is able to match the individual level data, except that the predicted distribution is more concentrated than the empirical distribution.

We conjecture that the discrepancies of the two distributions are caused by the following reasons. First, we restrict consumers to travel a maximum of 40 miles, but this mileage limit may be different across different individuals. Consider a consumer who does not travel more than 30 miles to buy a car. Suppose that within 40 miles of her residence, there are two dealers: one is 1 mile away and the other is 35 miles away. Since she only considers dealers within 30 miles, she will choose the first dealer for sure and her traveling distance in the data will be just 1 mile. However, the model

assumes that all consumers will consider all dealers within 40 miles and it will predict positive probabilities for both dealers and as a result, her predicted distance will be larger than her actual. This can explain why the empirical CDF is above the model CDF on the segment of small distance. Second, consumer search cost may not linear in the traveling distance. The distance function could concave, or more likely a step-function. As a result, a model with a linear approximation of the search cost will over-predict the search cost when the distance is large, and hence tend to predict that consumers travel shorter than the actual on the segment of large distance.

Figure 2: Predicted and Empirical Distributions of Traveled Distance



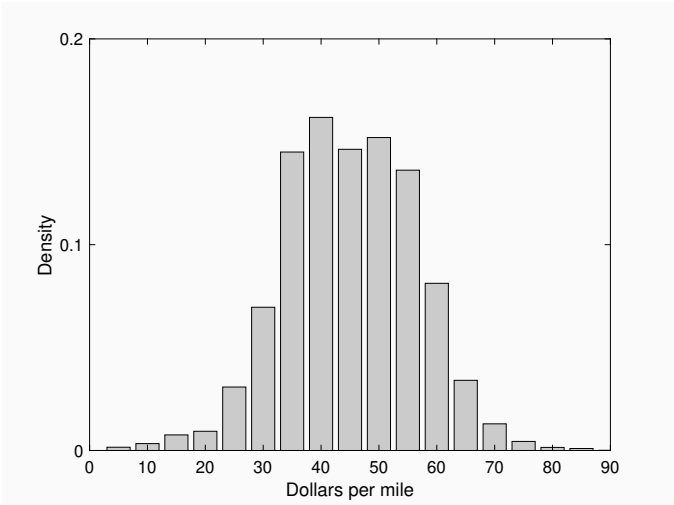
Note: The solid line represents the cumulative distribution of the actual traveling distance of the individual buyers that we have used to construct the likelihood function in the first stage estimation. The dashed line represents the cumulative distribution of their traveling distance predicted by the model.

4.3 Implied Search Cost

To get a sense of the economic magnitude of the parameter estimates, it is useful to consider how much a product's price needs to be lowered in order to compensate consumers if they have to travel one more mile. To do that, for each product we first calculate the sales change if it was one mile away from every consumer. Then, we calculate how much the price would need to be lowered to compensate the same sales loss. Figure 3 demonstrates the distribution of dollars per mile. Our results suggest that the average value is $45, and there is substantial heterogeneity across individuals.

Our estimate of the travel cost is lower than those reported in other studies that estimate consumer distance costs in the new car retail industry. For example, Moraga-González et al. (2015), the closest paper to ours, report a median travel cost of €107 per kilometer. The difference could come from two reasons. First, Moraga-González et al. (2015) consider the market for cars in the Netherlands. It is reasonable to think that search costs are higher in Europe due to congestion and higher fuel price. Second, we observe individual-level choice and the exact locations of the buyer and seller, and hence our parameter estimates could reflect important micro level information captured

Figure 3: Distribution of Dollar Per Mile



in the co-variation of distance and purchase probabilities.[21]

Furthermore, we examine what the estimates imply about consumers' search intensity. In general, consumer search is limited. Our estimates suggest that among those consumers who search, 46.67% of them search only one cluster, 34.41% search two clusters, 18.68% search three clusters, and less than 1% of them search more than three clusters. These results are consistent with industrial reports and previous studies. For example, in a survey by DME Automotive, an industry consulting group, 47% of all new car buyers visited a single dealer before purchase.[22] Moraga-González et al. (2015) report that 47% of survey respondents in their consumer survey data searched one dealer. Although our model does not have empirical content regarding specifically how many dealerships are searched because search happens at the dealer cluster level, we can at least say that searching two or more clusters implies searching at least two dealers, and so our estimates of consumer search intensity are in general consistent with other sources.

5 Counterfactual Experiments

In this section, we use our estimation results to conduct two sets of counterfactual exercises. The goal of our first set of counterfactual exercises is to understand how search frictions affect the market outcomes. We examine how the market outcomes change when we change the values of those key parameters in the search cost equation while keeping other parameters unchanged. In the second set of counterfactual exercises, we examine the impact of dealer closure on remaining dealers. In particular, we decompose the total effect of a dealer closure into an agglomeration effect and a

[21] Consider that a consumer bought a Toyota Camry. Since Moraga-González et al. (2015) do not observe which dealer the consumer purchased from, they assume that she purchased it from the closest Toyota dealer. In contrast, we incorporate exact purchase distance information which may show that this consumer actually purchased from a further dealer than the closest Toyota dealer, see Table 3 for details.

[22] See http://www.dmeautomotive.com/announcements/1-in-6-car-buyers-skips-test-drive-nearly-half-visit-just-one-or-no-dealership-prior-to-purchase.

competition effect. Simulating a dealer closure is not only a clear way to decompose the competition and agglomeration forces at work in the model, but it also is a highly policy relevant exercise. As discussed in section 2.2, the recent U.S. financial crisis of 2007-2009 saw many retail exits ; however, the microeconomic effects of retail closure, the agglomeration effect in particular, have not been well documented. In order to do both types of counterfactual exercises, we first specify a supply-side model to describe the price setting of car dealers. This allows us to recover marginal retail costs and evaluate changes to market outcomes, including optimal prices, in counterfactual environments.

5.1 Retail Pricing

We assume that car dealers, who are multi-product firms, play a static Nash Bertrand pricing game by simultaneously setting the retail price for each of their cars in each year[23]. The total variable profit of dealer f is defined as

$$\pi_f(p_t) = \sum_{j \in \mathcal{J}_{ft}} (p_{jft} - mc_{jft}) q_{jf}(p_t),$$

where mc_{jft} is the constant marginal cost of product j sold by dealer f in year t. This marginal cost represents the wholesale (or "invoice") price of the car, along with other variable costs or benefits associated with car retailing, including the future warranty and service contracts for the car and the opportunity costs of the inventory management problem faced by the dealer. See Albuquerque and Bronnenberg (2012) and Murry (2015) for a discussion of wholesale prices and retailing costs.

Dealers simultaneously set prices to maximize their own profit, taking into account prices and attributes of competing dealers. The first order condition for a particular dealer that defines a Nash Equilibrium in prices is

$$q_{jf}(\mathbf{p}_t) + \sum_{j \in J_{ft}} (p_{jft} - mc_{jft}) \frac{\partial q_{jf}(\mathbf{p}_t)}{\partial p_{jft}} = 0. \tag{13}$$

Let $\triangle$ denote the demand price derivative matrix with the row $k = (j, f)$ column $k' = (j', f')$ element:

$$\triangle_{kk'} = \frac{\partial q_{jf}(\mathbf{p}_t)}{\partial p_{j'f't}} = \begin{cases} \sum_z b_{zt} \int (\bar{\alpha} + \alpha^{inc} y_{zt}) \mathcal{P}_{izjft} (1 - \mathcal{P}_{izjft}) dF_\varsigma(\cdot), & if\, k = k' \\ -\sum_z b_{zt} \int (\bar{\alpha} + \alpha^{inc} y_{zt}) \mathcal{P}_{izjft} \mathcal{P}_{izj'f't} dF_\varsigma(\cdot), & if\, k \neq k' \end{cases}$$

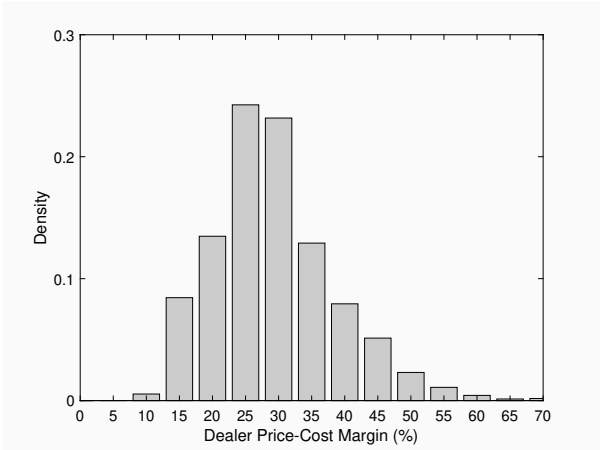
We define an ownership matrix Ω^*, with $\Omega(j, j')^* = 1$ if product j and j' are sold by the same dealer and zero otherwise. Let $\Omega = \Omega^* \times \triangle(p)$. Then, equation (13) can be written in matrix notation as the following markup equation

$$p - mc = \Omega^{-1} \mathfrak{q}(p). \tag{14}$$

[23]Price here is the same concept as in the demand model: the average price for each product at each dealer in each year. Because of our data is at the transaction level, we can construct average prices for a given model at a given dealer. Therefore, the price of a single product differs across dealers.

From equation (14), we compute the price-cost margins for each product sold by each dealer in each year, using the estimated demand parameters in Table (7). Figure 4 displays the distribution of dealer markups, defined as the ratio of price-cost margin over price. The weighted average markup (price-cost margin) is 29% and the median is 28%. These results are in line with other studies of the automobile industry, for example, 24% in Berry et al. (1995), 17% in Petrin (2002), $6,220 (price minus marginal cost) in Albuquerque and Bronnenberg (2012), $5,238 in Murry (2015), and 43% in Nurski and Verboven (2016) and Moraga-González et al. (2015).

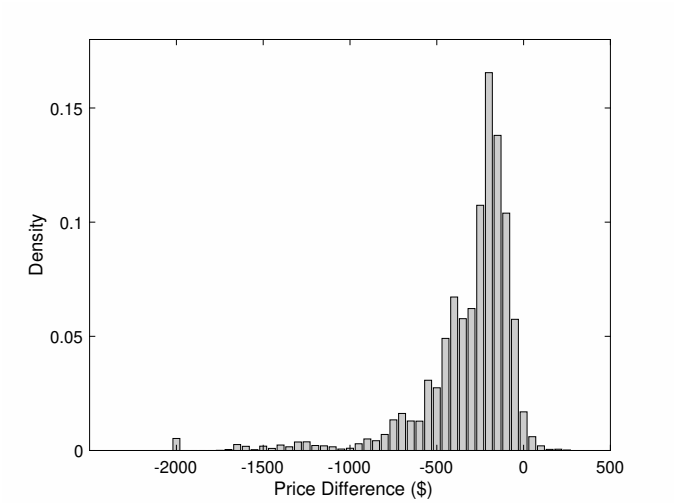
Figure 4: Predicted Dealer Markup (%)



5.2 Impacts of Search Frictions

To quantify the impact of search frictions, we simulate the market outcomes assuming that consumers have full information along with the estimated preference parameters in Table 7. One way to do this in our model is the following: recall from Section 4 that when $\gamma = 0$, $\rho = 0$ and $\kappa = 1$, the individual choice probabilities from our search model are equivalent to those from a full-information model with a mean utility from outside option being $log(2)$. Using this logic, our simulation results imply that in the full-information case, the total sales will be 33% higher than the sales predicted by our search model, and the weighted average price will be $333 lower. Figure 5 presents the distribution of the difference between the product-dealer-year level price predicted by the full-information model and that predicted by the search model. The standard deviation is $367, indicating that the price impacts caused by the search frictions are significantly different across products and dealers.

Figure 5: Price Difference in a Full-Information Model



Next, we simulate the equilibrium price and sales by varying features of the search cost: the effect of distance,γ, the standard deviation of search cost shocks κ, and the dealer cluster size coefficient ρ, while holding other model parameters at their estimated values in Table 7. We report the price and sales impacts in Table 8 and Table 9.

In Panel (I), we report the results when we scale γ from the estimated values from 0 to twice while keeping other parameters equal to their estimates. The weighted average price will be lower (higher) and total sales will be higher (lower) as we scale down (up) γ. This is expected since a higher γ discourages consumers to visit those dealers who are further away from their residence and leads to greater local monopoly power, and hence higher prices, for dealers because nearby residents are more captive.[24] In particular, when consumers' disutility from distance doubles the estimated value, the weighted average price will be \$84 higher and the total sales will be 32% lower than the predicted when γ equals to the estimated value. The standard deviation of the price difference is \$218, indicating a significant heterogeneity across products and dealers. In contrast, when consumers have no disutility from distance, the weighted average price will be \$109 lower and the total sales will be 38% higher than the case when γ equals to the estimated value.

Panel (II) reports the price and sales impacts when we scale κ from 0.1 to four times of the estimated value while keeping other parameters equal to their estimates. The weighted average price will be higher (lower) and the total sales will be lower (higher) when we scale down (up) κ, which is consistent with our analysis in section 3.4. A larger κ implies more randomness in consumers' choice of which clusters to search. Consequently, a dealer's location is less relevant in consumers' choice and this reduce dealers' local monopoly power. For example, compared with the predicted price and sales with κ at its estimated value, the weighted average price will be \$68 lower with a standard deviation of \$161, and the total sales will be 17% higher when κ is four times of its estimated value. In contrast, when κ is 0.1 of its estimated value, the weighted average price will

[24]Less search also results in worse matches which will put downward pressure on prices, but we find that the information rents dominate.

be \$104 higher with a standard deviation of \$281, and the total sales will be 10% lower.

Panel (III) reports the results when we set ρ (the coefficient before the number of dealers in a cluster) to various values from 0 to 0.8. A larger ρ implies that consumers pay larger search costs, resulting in less search, worse matches, and lower sales. Moreover, a larger ρ discourages consumers to travel to search those larger but further clusters, leading greater local monopoly power and hence higher prices for nearby dealers. The effect of the higher price reinforces the decrease in total sales. For example, when ρ equals to 0.2, the weighted average price will be \$244 higher with a standard deviation of \$199, and the total sales will be 66% lower than that when ρ equals to its estimated value.

Table 8: Price Difference by Varying Search Cost Parameters

Panel (I): Varying γ			Panel (II): Varying κ			Panel (III): Varying ρ		
Scale of $\hat{\gamma}$	Mean	SD	Scale of $\hat{\kappa}$	Mean	SD	Value of ρ	Mean	SD
0	-\$109	(\$216)	0.1	+\$104	(\$281)	0.1	\$143	(\$127)
0.25	-\$90	(\$181)	0.5	+\$53	(\$127)	0.2	\$244	(\$199)
0.50	-\$61	(\$130)	1.5	-\$28	(\$68)	0.3	\$314	(\$259)
0.75	-\$29	(\$67)	2	-\$44	(\$105)	0.4	\$365	(\$306)
1.25	+\$26	(\$65)	2.5	-\$54	(\$128)	0.5	\$404	(\$344)
1.50	+\$49	(\$123)	3.0	-\$60	(\$143)	0.6	\$438	(\$377)
1.75	+\$69	(\$175)	3.5	-\$64	(\$154)	0.7	\$460	(\$404)
2	+\$84	(\$218)	4	-\$68	(\$161)	0.8	\$481	(\$427)

Note: Price difference is the difference in the sales-weighted average price between a model with the stated paremeter changed and a model with all paraemters equal to their estimated values reported in Table 7.

Table 9: Total Sale Change by Varying Search Cost Parameters

Panel (I): Varying γ		Panel (II): Varying κ		Panel (III): Varying ρ	
Scale of $\hat{\gamma}$	Change	Scale of $\hat{\kappa}$	Change	Value of ρ	Change
0	+38%	0.1	-10%	0.1	-44%
0.25	+31%	0.5	-7%	0.2	-66%
0.50	+22%	1.5	+6%	0.3	-78%
0.75	+11%	2	+10%	0.4	-85%
1.25	-10%	2.5	+13%	0.5	-89%
1.50	-18%	3.0	+15%	0.6	-92%
1.75	-25%	3.5	+16%	0.7	-94%
2	-32%	4	+17%	0.8	-95%

Note: The total sales change is the change of the total units sold predicted by a model with the stated paremeter changed from that predicted by a model with all paraemters equal to their estimated values reported in Table 7.

5.3 Single Dealer Closure

Next we use our structural model to study the effects of closing a single dealer. As we have discussed above, our proposed model implies that closing a dealership generates two effects to the remaining

dealers located in the same cluster. On one hand, a closure may reduce the total attraction of the cluster, and thus reduce the sales of other dealers in this cluster through decreased consumer search. This effect puts pressure on dealers to reduce their prices to counter the negative impact of reduced search because lower prices attract more searching consumers. This is the "agglomeration effect". On the other hand, closing a dealer would directly reduce the price competition among dealers in the same cluster, and create an incentive for higher equilibrium prices. This is the "competition effect".

We consider a hypothetical scenario in which a single dealer was closed in 2007. The two dealers we consider are two of the largest dealers in 2007, labeled as Dealer A and Dealer B. Dealer A's share in its cluster was between 10% and 20%, while Dealer B's share in its cluster was above 50%.[25] To separately quantify the agglomeration and competition effects of dealer co-location, we simulate changes to equilibrium prices and sales for the following three scenarios. In the first scenario, we quantify the agglomeration effect by allowing consumers to respond to the dealer closure by adjusting only the choice of each search set ($\mathcal{P}_{izS}$), but not the choice probability of purchasing each product conditional on a search set ($\mathcal{P}_{izjft|S}$). In this scenario, retailers adjust their prices only for the reason to attract new searchers to their dealer cluster but not to compete against a rival in the same geographic cluster. In the second scenario we quantify the competition effect by allowing consumers to respond to the dealer closure by adjusting only the choice of car conditional on a search set ($\mathcal{P}_{izjft|S}$), but not the choice of clusters to search ($\mathcal{P}_{izS}$). Accordingly, retailers will adjust their prices to compete with local rivals but not to attract more consumers to search their geographic cluster. In the last scenario we allow consumers to respond to the closure by adjusting both their choice sets and the choice of car conditional on the choice set, which quantifies the total effect.

Table (10) reports the impacts of closing a dealer on the price, total sales, and total profit of two groups of dealers. The first group of dealers are those who are colocated with the closed dealer, and the second group includes all other dealers that are not located in the cluster where the closed dealer was located. In each counterfactual scenario, we simulate the equilibrium price and sales and compute the profit for each product-dealer combination. We take the difference of the simulated price over the observed price for each product-dealer. Then, we compute the sales-weighted average and standard deviations, and we report the results in the first and second columns. We also compute the total sales and total profit in the counterfactual scenario, and report the differences over the observed ones in the third and forth columns.

Due to the agglomeration effect, closing Dealer A or Dealer B will reduce the total attractiveness of the cluster and hence reduce the total sales of other co-located dealers (-10% and -26%). Moreover, the closure will also induce the co-located dealers to reduce their prices to counter the reduced attractiveness of the cluster (-\$8 and -\$40). Therefore, our results imply that in both cases of closing Dealer A and closing Dealer B, the agglomeration effect is positive, that is, the cluster of

[25] Our point here is to illustrate how large the agglomeration and competition effects can be if an "anchor" store closes. Of course, if a small dealer is closed both effects will be much smaller, although the net effect could go either way.

the closed dealer will be less likely included in consumers' search set. On the other hand, due to the competition effect, colocated dealers will be able to charge higher prices and sell more when a nearby rival exits. Other dealers not located in the same cluster will benefit from the closure both because their clusters become more attractive to consumers to visit but also because the competition becomes less intense. Unsurprisingly, the effects on non-located dealers are much smaller than on those colocated dealers because .

Moreover, since Dealer B plays a larger role in its cluster than Dealer A, closing Dealer B will have larger impacts on co-located dealers through both agglomeration and competition effects. Taking these two effects together, closing Dealer A has a net negative effect on the incumbent dealers, suggesting the agglomeration effect dominates in this case. However, closing Dealer B will slightly benefit the colocated dealers, suggesting the competition effect dominates in this case.

Table 10: Impacts of Closing One Dealer

(a) Closing Dealer A

	Price		Total sales	Total profit
Co-located Dealers				
Agglomeration Effect	-\$8.78	(\$5.16)	-10.94%	-11.05%
Competition Effect	+\$10.93	(\$5.52)	+8.80%	+8.97%
Total Effect	+\$1.06	(\$0.24)	-3.15%	-3.14%
Non - Co-located Dealers				
Agglomeration Effect	+\$0.46	(\$1.95)	+0.28%	+0.27%
Competition Effect	+\$0.17	(\$0.89)	+0.17%	+0.16%
Total Effect	\$0.62	(\$2.66)	+0.43%	+0.42%

(b) Closing Dealer B

	Price		Total sales	Total profit
Co-located Dealers				
Agglomeration Effect	-\$40	(\$37)	-26.42%	-26.08%
Competition Effect	+\$502	(\$206)	+87.08%	+97.43%
Total Effect	+\$451	(\$131)	+34.29%	+41.05%
Non - Co-located Dealers				
Agglomeration Effect	+\$5.05	(\$21.44)	+0.49%	+0.55%
Competition Effect	+\$3.14	(\$19.54)	+0.28%	+0.32%
Total Effect	+\$8.03	(\$37.08)	+0.71%	+0.82%

Note: The first columns report the sales weighted average of the price difference at the product-dealer level between the counterfactual scenario and the data. The second columns report the standard deviation of that price difference. The third columns report the difference in total sales between the counterfactual scenario and the data. The forth columns report the difference in total profit between the counterfactual scenario and the data.

5.4 Terminations of Pontiac and Saturn

In this section, we focus on the termination of Pontiac and Saturn in 2009. Since the brand terminations were national wide decisions, the dealer closures caused by the brand terminations

were plausibly not correlated with the local conditions. We first simulate the market price and sales for other dealers in 2007 by hypothetically assuming that the termination of Pontiac occurred before 2007, and then compare the simulated outcomes with the observed ones. We do the same simulations by assuming Saturn was closed in 2007. We decompose the effect of closures in the agglomerations effect, competition effect, and total effect like in the previous exercise in Section 5.3.

Table 11(a) and 11(b) report the impacts of closing Pontiac and Saturn on the price, total sales, and total profit of the colocated dealers and non-colocated dealers. On the one hand, the agglomeration effect implies that those clusters would be less attractive to consumers and hence would reduce the total sales of those clusters. To counter this effect, the colocated dealers in those clusters would cut their prices. Our simulation results suggest that due to the agglomeration effect, hypothetically closing Pontiac would induce the dealers co-located with Pontiac dealers to cut their prices by $19 per car on average. Their total sales would be 2.14% lower and their profit would be 2.31% lower. Meanwhile, the weighted average price, the total sales and profit of the dealers in other clusters would be higher, because those clusters become more attractive to consumers. In the counterfactual scenario of closing Saturn, the colocated dealers suffer even more and the non-colocated dealers benefit less, indicating that the agglomeration effect is stronger in this counterfactual scenario. In short, we find that the agglomeration effect is positive in both counterfactual experiments of Pontiac closure and Saturn closure. Therefore, a full-information model that ignores the agglomeration effect would definitely overstate the positive impact of dealer closure on remaining colocated dealers.

On the other hand, closing a brand benefits co-located dealers because fewer competitors implies larger market power and more sales. In the counterfactual scenario of closing Pontiac, those colocated dealers would slightly increase their price and their total sales would be 3.24% higher. As a result, their profit would be 3.2% higher. Meanwhile, those non-colocated dealers would be also better off due to the lower competition, although they benefit less than the colocated dealers would. Similarly, colocated dealers and non-colocated dealers would be better off when we hypothetically close Saturn.

Taking these two effects together, closing Pontiac would make the colocated dealers slightly better off, whereas closing Saturn would slightly reduce the total profit of the colocated dealers. Our results imply that the competition effect dominates when Pontiac was closed whereas the agglomeration effect dominates when Saturn was closed. This is quite different to the findings of other studies on dealer closures following the financial crisis. For example, Ozturk et al. (2016) find evidence that the competition effect dominates when Chrysler closed dealers in 2010. Benmelech et al. (2014) document massive retail exits during the financial crisis due to financial reasons, such as bankruptcy and find evidence for an agglomeration effect of dealer closure.[26]

The difference in the results between Pontiac and Saturn are intuitive given that these brands had much different retailing arrangements. In Ohio, 16 out of 20 dealers selling Saturn were single-

[26]For example, they document the complete liquidation of multiple large retailers, including Circuit City, Linens 'N Things, and The Sharper Image. Other large retail chains that experienced massive closings due to financial trouble include Kmart and Sears.

brand dealers, whereas 18 out of 76 dealers selling Pontiac were single branded. Partly because of that, Saturn dealers were of more importance within the clusters where they located than Pontiac dealers. For example, Saturn's actual sales accounted more than 12% of all sales in their clusters, whereas Pontiac's within-clusters share was 8%. As a result, closing Saturn would have larger impacts on colocated dealers both through the agglomeration effect and through the competition effect, which has been shown in Table 11. Moreover, the agglomeration effect would outperform the competition effect on colocated dealers when Saturn was closed.

Table 11: Impacts of Brand Closures

(a) Closing Pontiac

	Price		Total sales	Total profit
Colocated Dealers				
Agglomeration Effect	-\$19	(\$62)	-2.14%	-2.31%
Competition Effect	+\$2	(\$51)	+3.24%	+3.20%
Total Effect	-\$3	(\$58)	+0.92%	+0.87%
Non-Colocated Dealers				
Agglomeration Effect	+\$9	(\$10)	+1.56%	+1.68%
Competition Effect	+\$7	(\$6)	+1.46%	+1.54%
Total Effect	+\$15	(\$15)	+2.90%	+3.10%

(b) Closing Saturn

	Price		Total sales	Total profit
Colocated Dealers				
Agglomeration Effect	-\$10	(\$17)	-4.44%	-4.57%
Competition Effect	+\$15	(\$18)	+4.49%	+4.70%
Total Effect	+\$5	(\$16)	-0.24%	-0.17%
Non-Colocated Dealers				
Agglomeration Effect	+\$6	(\$7)	+1.35%	+1.39%
Competition Effect	+\$3	(\$4)	+1.18%	+1.20%
Total Effect	+\$9	(\$10)	+2.42%	+2.48%

Note: The first columns report the sales weighted average of the price difference at the product-dealer level between the counterfactual scenario and the data. The second columns report the standard deviation of that price difference. The third columns report the difference in total sales between the counterfactual scenario and the data. The forth columns report the difference in total profit between the counterfactual scenario and the data.

6 Conclusion

In this paper, we present a structural model of consumer search for spatially differentiated products in the new car retail industry. The model explicitly captures the agglomeration and competition effects of retail co-location. We estimate the model using detailed data on all new car transactions in a single U.S state. Our approach contributes to the literature on consumer demand with limited information and the literature on retail agglomeration.

Our results indicate that consumers' search cost is \$45 per mile on average and due to the substantial search cost, search is very limited. We also show that the average price-cost markup is \$333 higher due to the presence of search frictions. Moreover, our counterfactual analysis suggests that both the competition and agglomeration effects matter after a dealer closure. We show that the agglomeration effect becomes stronger when consumers get larger disutility from traveling distance or when their choice of which cluster(s) to search becomes less random. In general, the results suggest that substitution pattern across dealer clusters is crucial for understanding the tradeoff between agglomeration and competition. We think this insight is an important result that can help inform policy makers and managers about the effects of co-location and contagion of retail closures.

Our main finding is that the agglomeration effect is positive: there are negative effects on dealers of a co-located dealer closure. Because competition also plays a role, we find cases where there exists only moderate negative net effects of closures on co-located dealers and some cases where the competition effect dominates and closures are a net positive for co-located incumbents. However, our finding that the agglomeration effect could dominate the competition effect has important implications for policy-makers and managers. For example, our results rationalize the co-location of rivals and suggest that co-located stores act (partially) as complements and, as such, rivals may not want to force closures. Also, the results suggest that if the agglomeration effect dominates then local governments who often help organize retail landscapes should be worried about closure spirals, as each retail closure has a net negative effect on remaining stores.

To be sure, our analysis relies on particular assumptions. Although we are confident that our model captures the major features of this industry, some caveats are worth mentioning. First, although the evidence we present suggests dealer agglomeration is an important consideration during consumers' car buying process, the search process in reality may be more complicated than our model presents. In particular, the recent proliferation of car-buying websites that aim at alleviating consumer information has likely started to change the way consumers search for cars. However, cars are experience goods, so websites could never fully inform a consumer completely about the utility as personal interaction can. Second, consumers may search in a more complicated way, for example, nesting geographical concerns with the search for a dealer (as in Moraga-González et al. (2015)) and the search for a car type. Because we do not observe search behavior explicitly, we are unable to separately identify different search mechanisms. Thirdly, although we present a demand-driven reason for dealers to co-locate, there are likely cost-driven reasons, for example land prices, zoning, and management convenience for multi-dealership dealer conglomerates. Our analysis is not a full equilibrium analysis of retail location decisions and cannot be used to balance all the tradeoffs associated with the optimal location decision. Instead, we focus on identifying the importance of demand side motives that have been identified in the theoretical literature as being important determinants of co-location. Lastly, there may be important dealer-time unobserved heterogeneity that we did model, for example weekly/monthly advertising by dealers might

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Appendix A: Proofs of Proposition 1 and 2

[Proof of proposition 1]:

Without loss of generality, we will show the proposition holds for cluster 1.

The probability of visiting a firm in cluster 1 is

$$\mathcal{P}_1 + \mathcal{P}_{1\&2} \quad = 1 - \quad \frac{e^{\kappa} + \frac{n_2 e^{\mu}+1}{e^{(\gamma d_2+\rho n_2)}}}{e^{\kappa} + \frac{n_1 e^{\mu}+1}{e^{(\gamma d_1+\rho n_1)}} + \frac{n_2 e^{\mu}+1}{e^{(\gamma d_2+\rho n_2)}} + \frac{(n_1+n_2)e^{\mu}+1}{e^{\gamma(d_1+d_2)+\rho(n_1+n_2)}}}.$$

Let Γ denote the denominator $e^{\kappa} + \frac{n_1 e^{\mu}+1}{e^{(\gamma d_1+\rho n_1)}} + \frac{n_2 e^{\mu}+1}{e^{(\gamma d_2+\rho n_2)}} + \frac{(n_1+n_2)e^{\mu}+1}{e^{\gamma(d_1+d_2)+\rho(n_1+n_2)}}$. Then we have

$$\frac{d(\mathcal{P}_1 + \mathcal{P}_{1\&2})}{dn_1} = \frac{e^{\kappa} + \frac{n_2 e^{\mu}+1}{e^{(\gamma d_2+\rho n_2)}}}{\Gamma^2} \frac{d\Gamma}{dn_1}.$$

Here,

$$\begin{aligned} \frac{d\Gamma}{dn_1} &= \frac{e^{\mu} - (n_1 e^{\mu}+1)\rho}{e^{(\gamma d_1+\rho n_1)}} + \frac{e^{\mu} - [(n_1+n_2)e^{\mu}+1]\rho}{e^{\gamma(d_1+d_2)+\rho(n_1+n_2)}} > 0 \\ \Leftrightarrow \quad & [(n_1+n_2)e^{\mu}+1]\rho + (n_1 e^{\mu}+1)\rho e^{\gamma d_2+\rho n_2} < (1+e^{\gamma d_2+\rho n_2})e^{\mu}. \end{aligned}$$

First, the above inequality holds when $\rho = 0$. Second, the left hand side is clearly above the right hand side when ρ goes to infinity. Third, the left hand side is an increasing function of ρ. Hence, there must exists a positive cutoff ρ^* such that as long as $\rho < \rho_1^*$, $\frac{d\Gamma}{dn_1} > 0$ and hence $\frac{d(\mathcal{P}_1+\mathcal{P}_{1\&2})}{dn_1} > 0$; otherwise, $\frac{d\Gamma}{dn_1} \leq 0$ and hence $\frac{d(\mathcal{P}_1+\mathcal{P}_{1\&2})}{dn_1} \leq 0$. Moreover, it is easy to show that the cutoff ρ_1^* is decreasing in n_1 and n_2.

[Proof of proposition 2]:

First, we can easily show that $\frac{d(\mathcal{P}_1+\mathcal{P}_{1\&2})}{dn_1} \to 0$ as $\kappa \to \infty$ and that $\frac{d(\mathcal{P}_1+\mathcal{P}_{1\&2})}{dn_1} > 0$ as $\kappa \to 0$.

We take partial derivative of the agglomeration effect $\frac{d(\mathcal{P}_1+\mathcal{P}_{1\&2})}{dn_1}$ with respect to κ.

$$\begin{aligned} \frac{d^2(\mathcal{P}_1 + \mathcal{P}_{1\&2})}{dn_1 d\kappa} &= \frac{e^{\kappa}}{\Gamma^3}\left[\Gamma - 2e^{\kappa}(e^{\kappa} + \frac{n_2 e^{\mu}+1}{e^{(\gamma d_2+\rho n_2)}})\right]\frac{d\Gamma}{dn_1} \\ &\propto \Gamma - 2e^{\kappa}(e^{\kappa} + \frac{n_2 e^{\mu}+1}{e^{(\gamma d_2+\rho n_2)}}) \\ &= -2(e^{\kappa})^2 - (2B-1)e^{\kappa} + A \end{aligned}$$

where $A \equiv \Gamma - e^{\kappa}$ and $B \equiv \frac{n_2 e^{\mu}+1}{e^{(\gamma d_2+\rho n_2)}}$.

Define $\kappa^* = ln\{\frac{\sqrt{(2B-1)^2+8A}-(2B-1)}{4}\}$. Then, $\frac{d^2(\mathcal{P}_1+\mathcal{P}_{1\&2})}{dn_1 d\kappa} \geq 0$ when $\kappa \leq \kappa^*$, and $\frac{d^2(\mathcal{P}_1+\mathcal{P}_{1\&2})}{dn_1 d\kappa} < 0$ when $\kappa > \kappa^*$.

Appendix B: Derivation of the Second-Stage Estimates

First stage. Estimated non-linear parameters $\hat{\theta}_1$ maximizes the log-likelihood function in equation (10). Asymptotically,

$$\sqrt{N_1}(\hat{\theta}_1 - \theta_1) \sim N(0, \Sigma).$$

Then, we obtain the estimated mean utilities $\hat{\delta}$ which is a function of estimated non-linear parameters $\hat{\theta}_1$, denoted as $\hat{\delta} = g(\hat{\theta}_1)$.

Let $C(\delta)$ denote the variance-covariance of δ. It is

$$C(\delta) = \left[\frac{\partial g(\hat{\theta}_1)}{\partial \theta_1}\right] \Sigma \left[\frac{\partial g(\hat{\theta}_1)}{\partial \theta_1}\right]' .$$

Here, $g(.)$ can be obtained from the contraction mapping $\Gamma(\delta, \theta_1) = 0$ that sets the predicted market shares equal to the observed market shares. Therefore,

$$\frac{\partial g(\hat{\theta}_1)}{\partial \theta_1} = -\left[\frac{\partial \Gamma(\delta, \theta_1)}{\partial \delta}\right]^{-1} \left[\frac{\partial \Gamma(\delta, \theta_1)}{\partial \theta_1}\right].$$

Second stage. Estimated linear parameters $\hat{\theta}_2$ solves the moment conditions (12). Asymptotically,

$$\sqrt{N_2}(\hat{\theta}_2 - \theta_2) \sim N(0, \Omega),$$

where Ω is the corrected covariance-variance of $\hat{\theta}_2$. Let $C(\xi)$ denote the covariance-variance of ξ . Then,

$$\Omega = (X' P_Z X)^{-1} X' P_Z [C(\xi) + C(\delta)] P_Z' X (X' P_Z' X)^{-1},$$

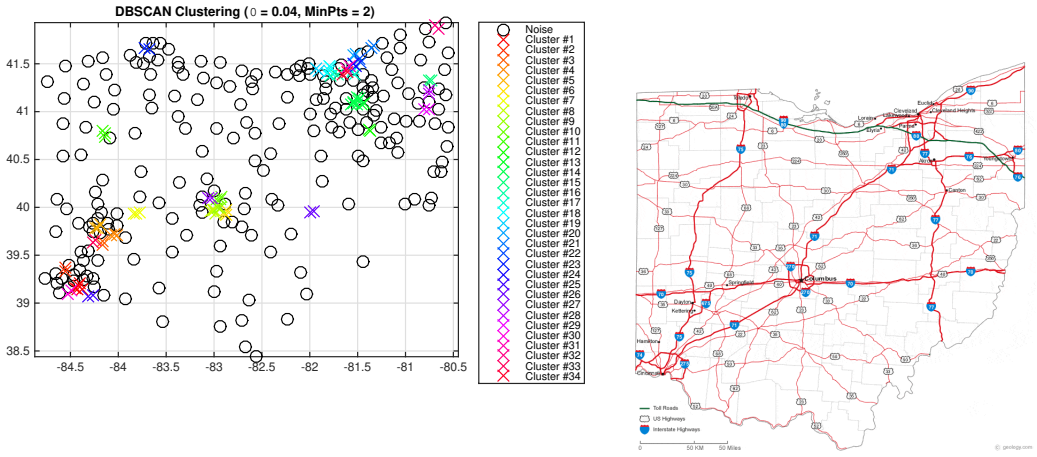
where $P_Z = Z(Z'Z)^{-1}Z'$ is the projection matrix.

Appendix D: Additional Figures and Tables

Figure D.1: First-Stage Price Regression

Variable		IV1	IV2	IV3	IV4
log (acceleration)	3.4567	0.0073	-1.1521	-2.5431	2.2650
	(0.1809)***	(0.0987)	(0.1081)***	(0.2069)***	(0.1061)***
log (car size)	-0.6958	-0.1468	1.2764	3.6415	3.3798
	(1.1531)	(0.1704)	(0.1525)***	(1.1667)***	(0.1463)
log (miles per dollar)	-0.5109	-0.2047	0.0207	-0.2437	-0.0279
	(0.0608)***	(0.1502)	(0.1505)	(0.1610)	(0.1473)
luxury brand	4.8530	-0.0139	-0.2454	-4.4358	0.8730
	(0.4045)***	(0.0513)	(0.0325)***	(0.3782)***	(0.2073)***
us brand	-2.1417	-0.1679	-0.0913	2.3655	0.9695
	(0.1540)***	(0.0326)***	(0.0223)***	(0.1543)***	(0.0994)***
Overall R square: 0.7131					
Weak identification test: Cragg-Donald Wald F statistic=1273.077					
Over-identification test: P-value=0.0000					

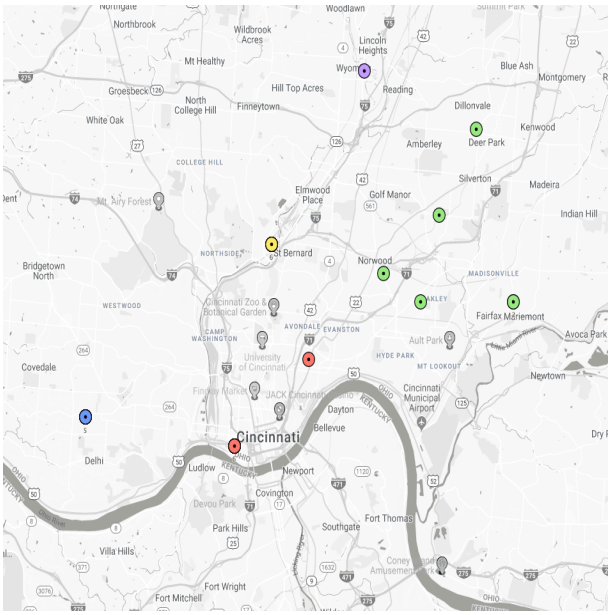
Note: Dealer fixed effect regression of price at the product-dealer-year level on the exogenous variables, including log of acceleration, log of car size, log of miles per dollar, luxury brand, U.S. brand, body style dummies, yearly dummies, and instrumental variables. IV1 are the deviations from the average characteristics of product-dealer combinations available in the same dealer cluster and in the same year, IV2 are the squares of IV1, IV3 are the deviations from the average characteristics of all product-dealer combinations in the same year, and IV4 are the squares of IV3. 101,371 product-dealer-year level observations. R^2=0.71.



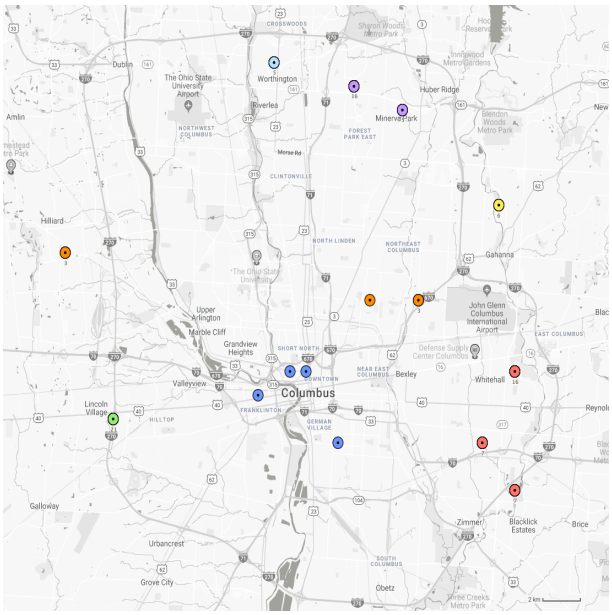
(a) Results of DBSCAN Clustering (b) Map of Ohio

Figure D.2: Spatial Distribution of Ohio Dealer Clusters

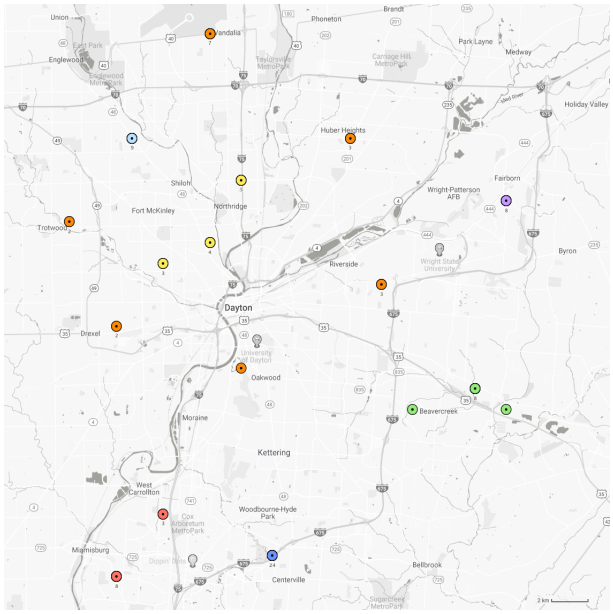
Note: The black dots indicate single-dealer clusters, and the colored crosses indicate multi-dealer clusters.



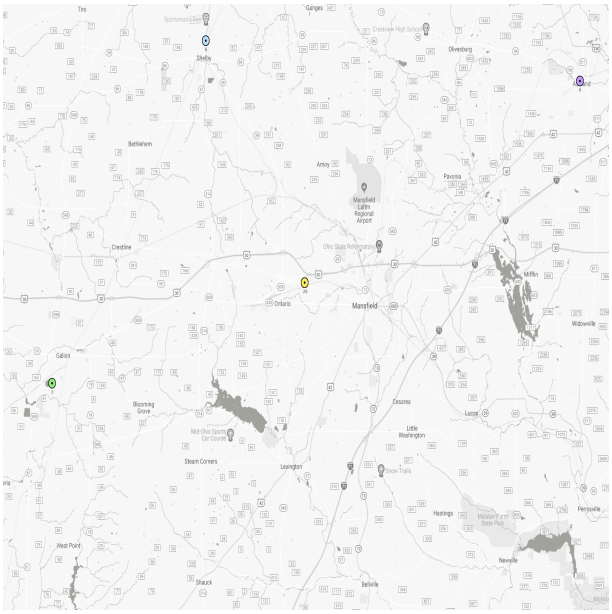
(a) Cincinnati, OH



(b) Columbus, OH



(c) Dayton, OH



(d) Mansfield, OH

Figure D.3: Dealer Cluster in Four Ohio Locations

Note: Each color groups together a unique dealer color, except for orange which always represents an isolated cluster. The number of brands represented by each dot is denoted under the dot.